

Sparse tensors are a natural way of representing real-world data



Kristina

★★★★☆ **Great Product**

March 30, 2017

Color: White | **Verified Purchase**

Great product. Large enough for all spoons and fits nicely on my stovetop. Would definitely buy it again.



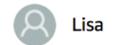
Teresa

★★★★★ **Excellent buy**

October 25, 2017

Verified Purchase

This is a great product for your boy who loves sports! It was a good value as well. Other stores sell for 3x the cost. I bought one for a basketball and football and my 9 year old loves it in his room. Solid item too, not flimsy. Will hold items nicely.



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December 5, 2017

Style: Battery Powered Alarm | Size: 1 Pack | **Verified Purchase**

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Recommended for you, Stephen



Snack Foods
15 ITEMS



Household Supplies
15 ITEMS



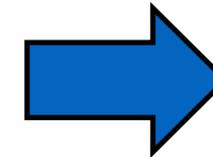
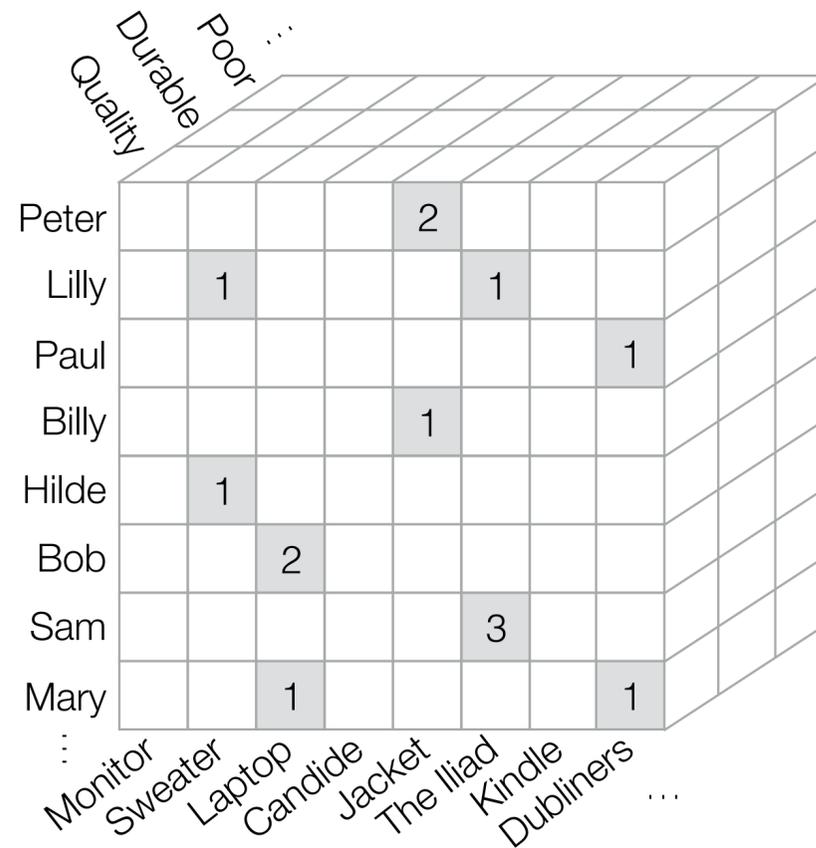
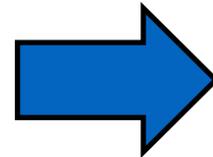
Janitorial & Sanitation Supplies
8 ITEMS



Candy & Chocolate
15 ITEMS

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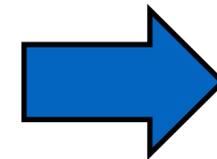
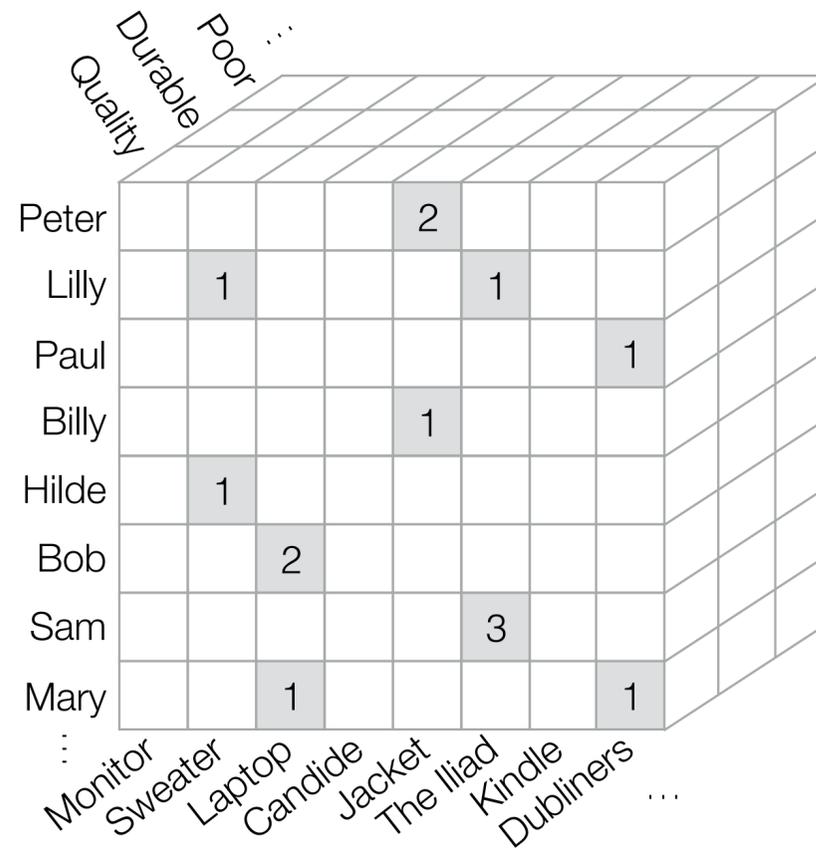
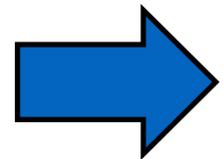
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15 ITEMS



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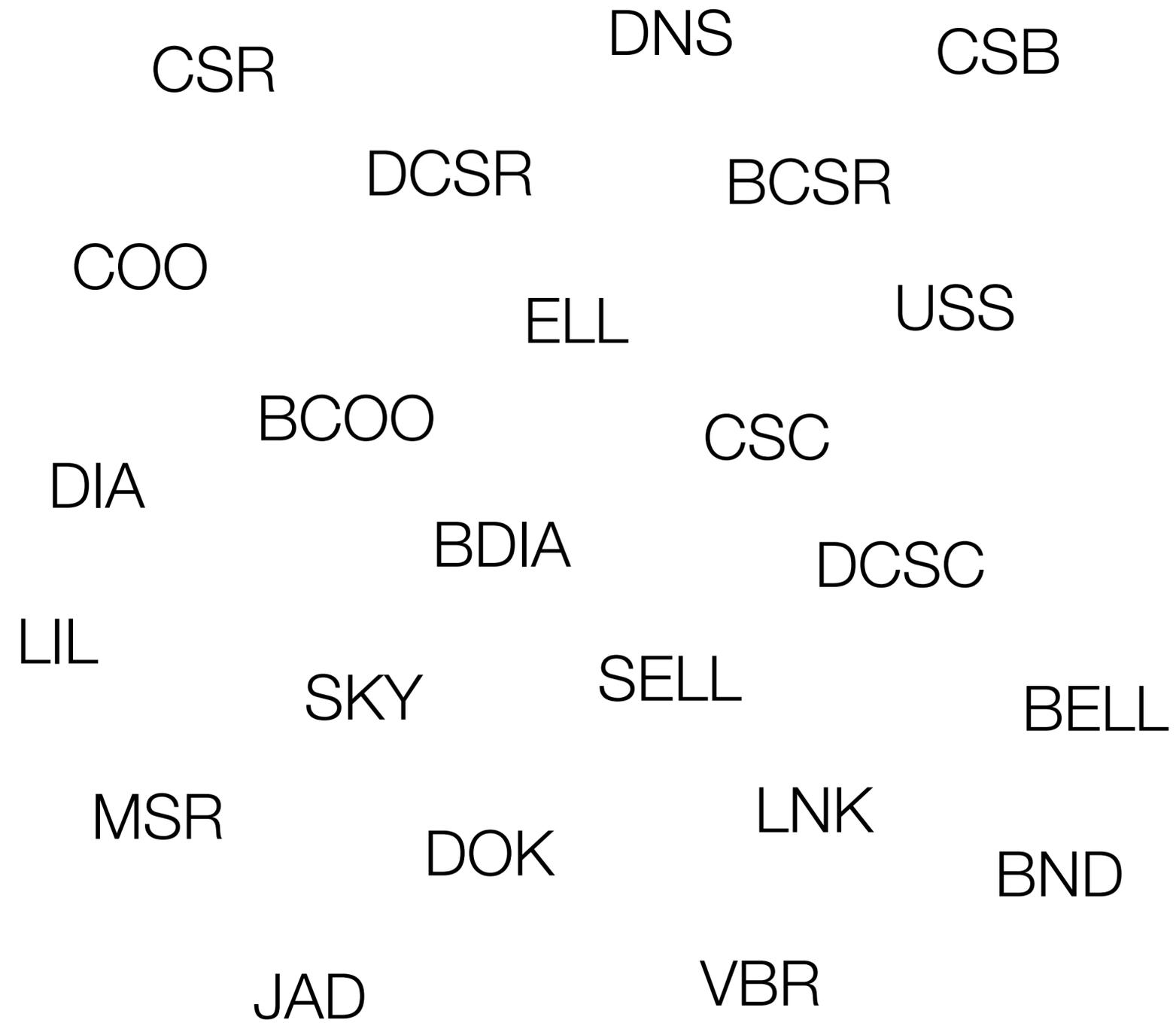
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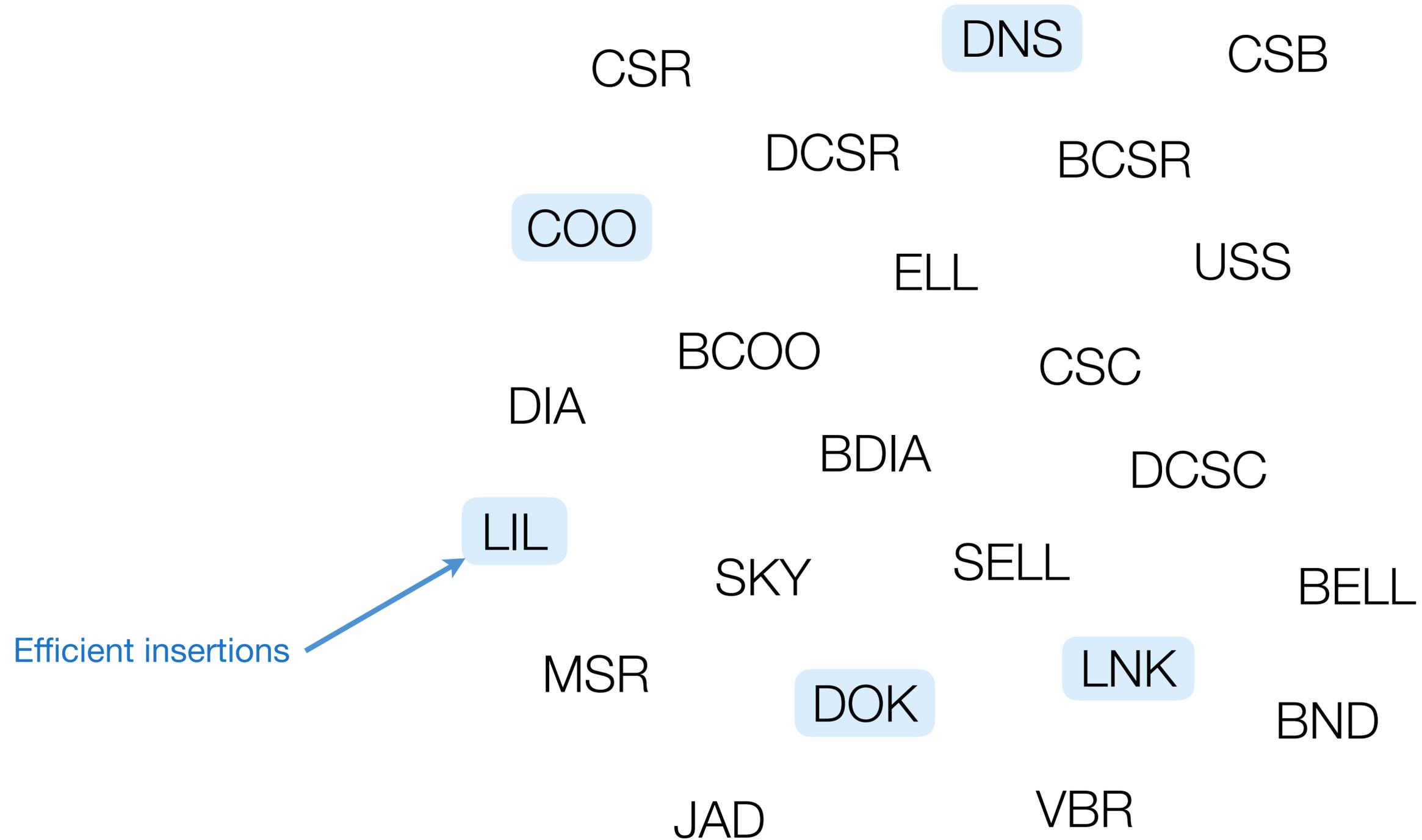
Candy & Chocolate
15 ITEMS

Dense storage: 107 exabytes
 Sparse storage: 13 gigabytes

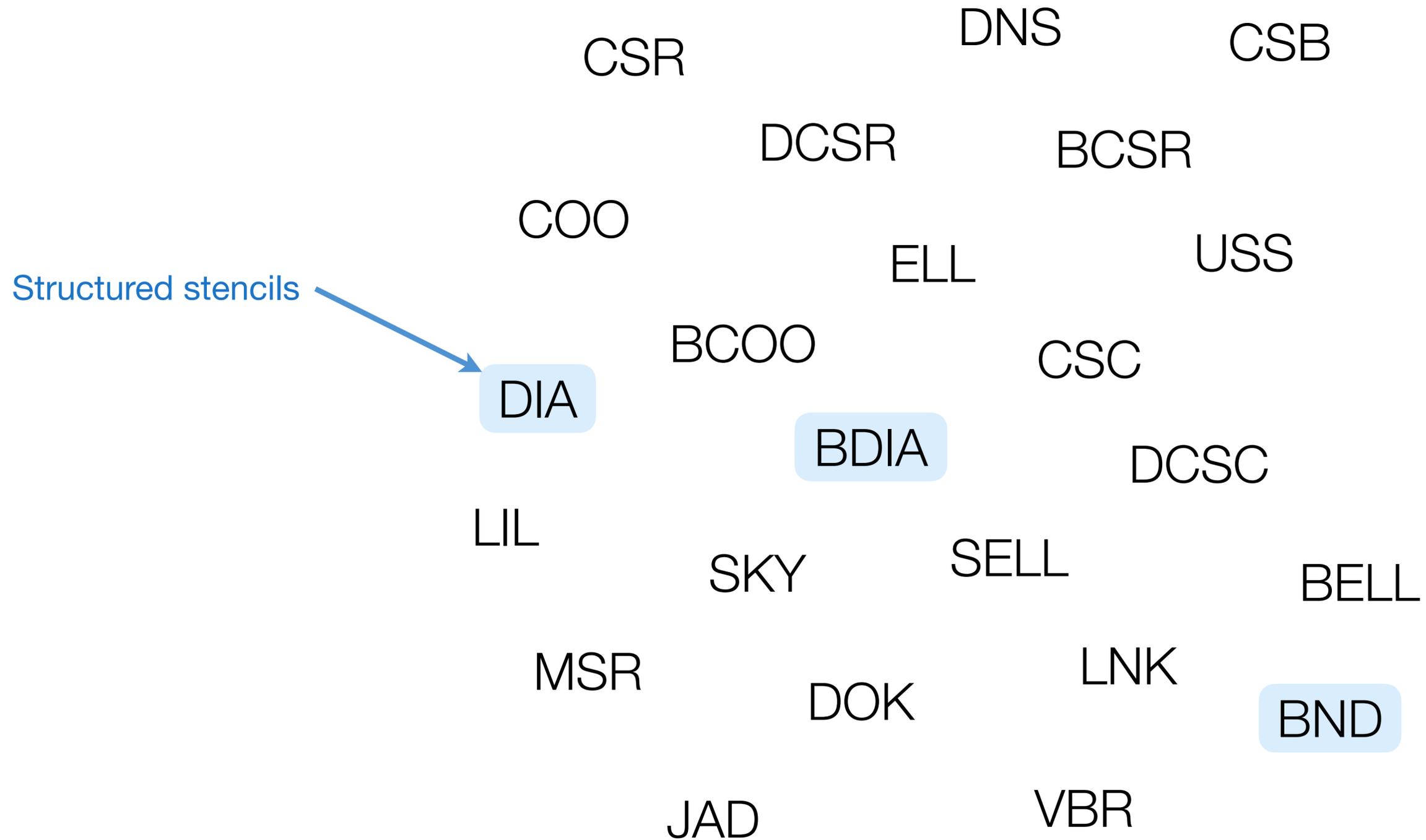
There exists many different formats for storing tensors



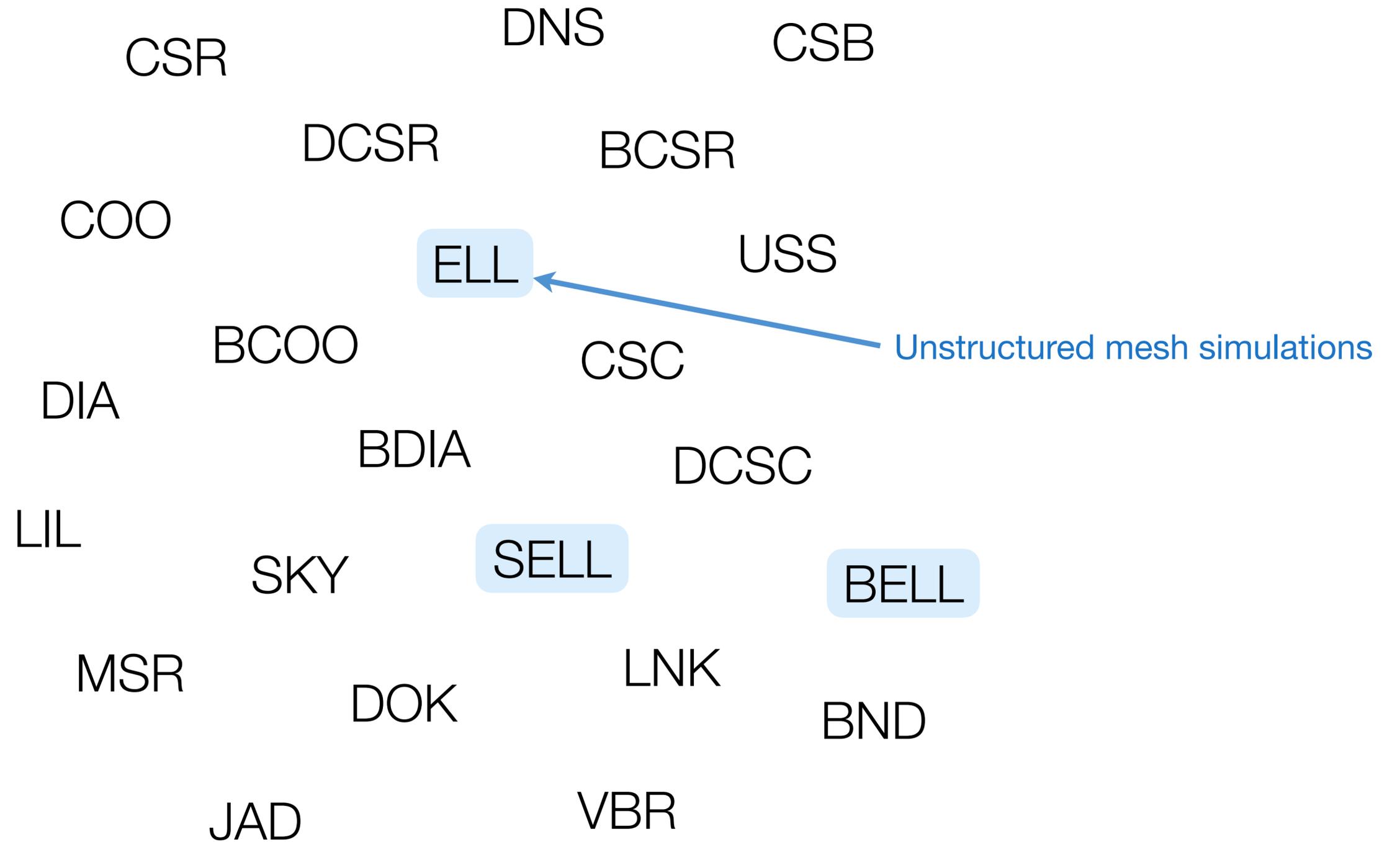
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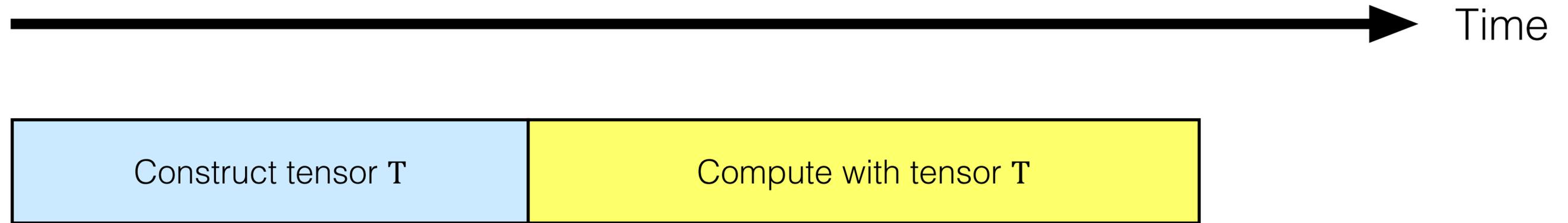
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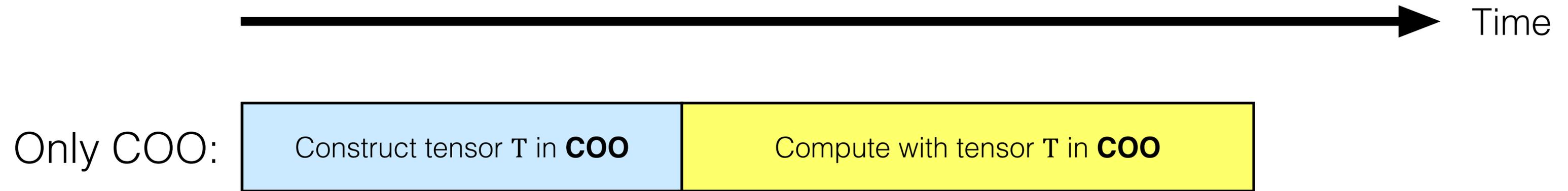
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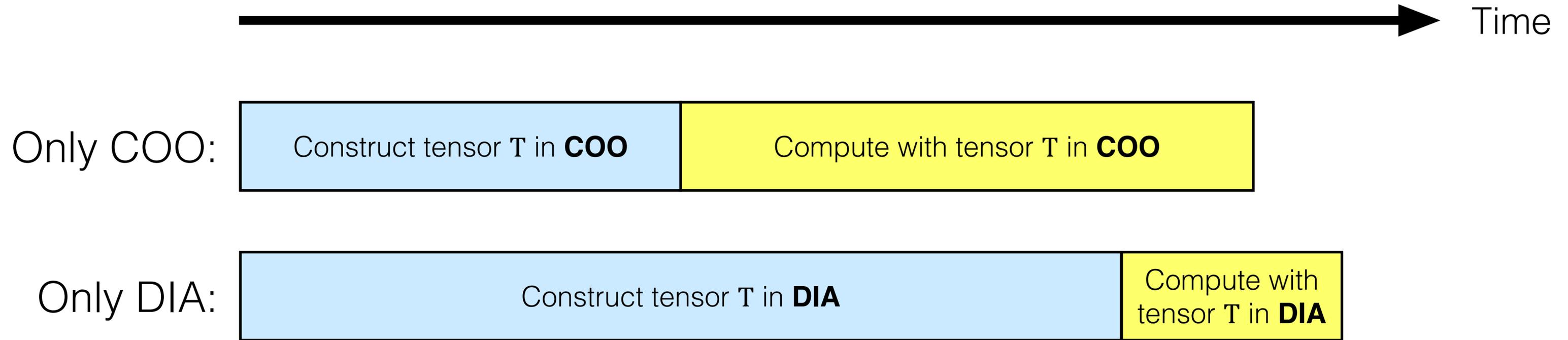
Applications must work with tensors in different formats for performance



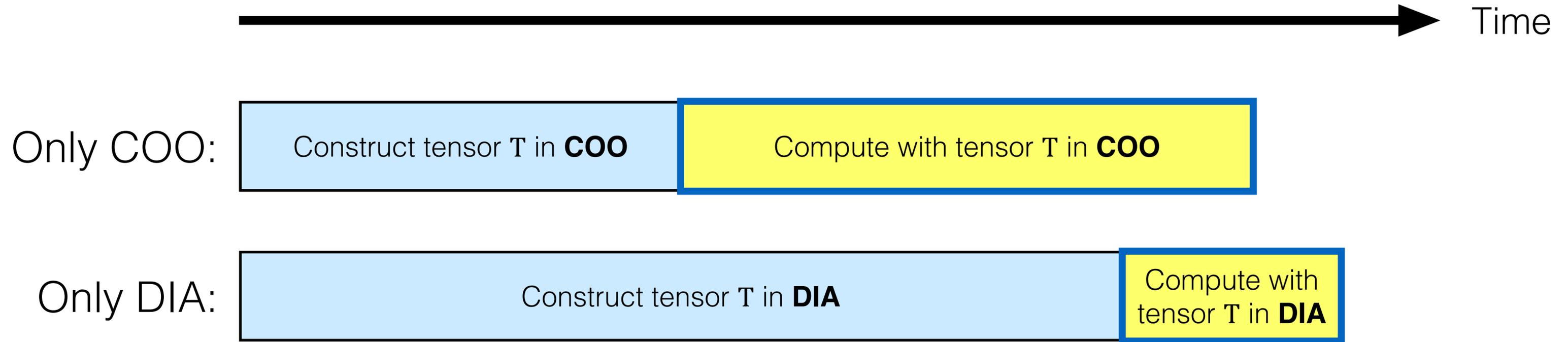
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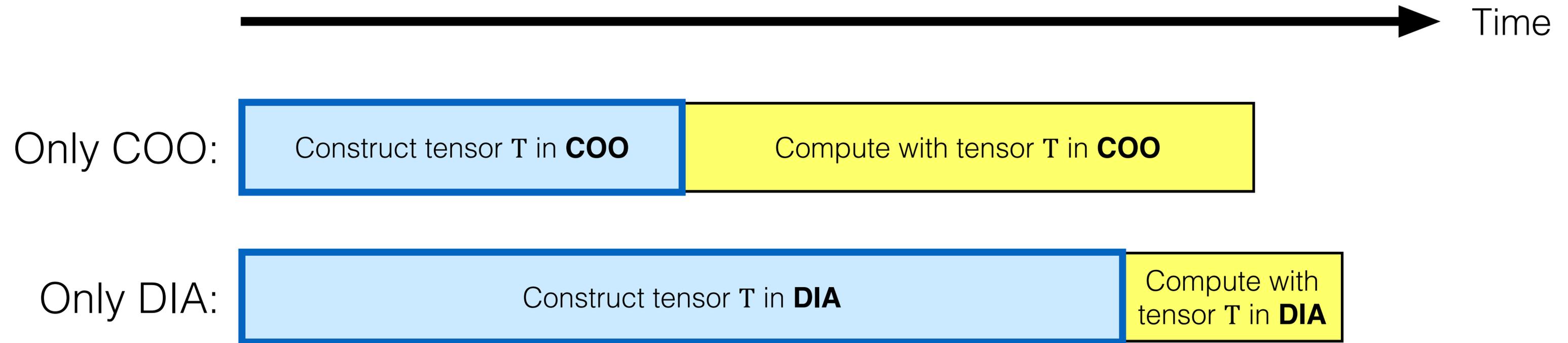
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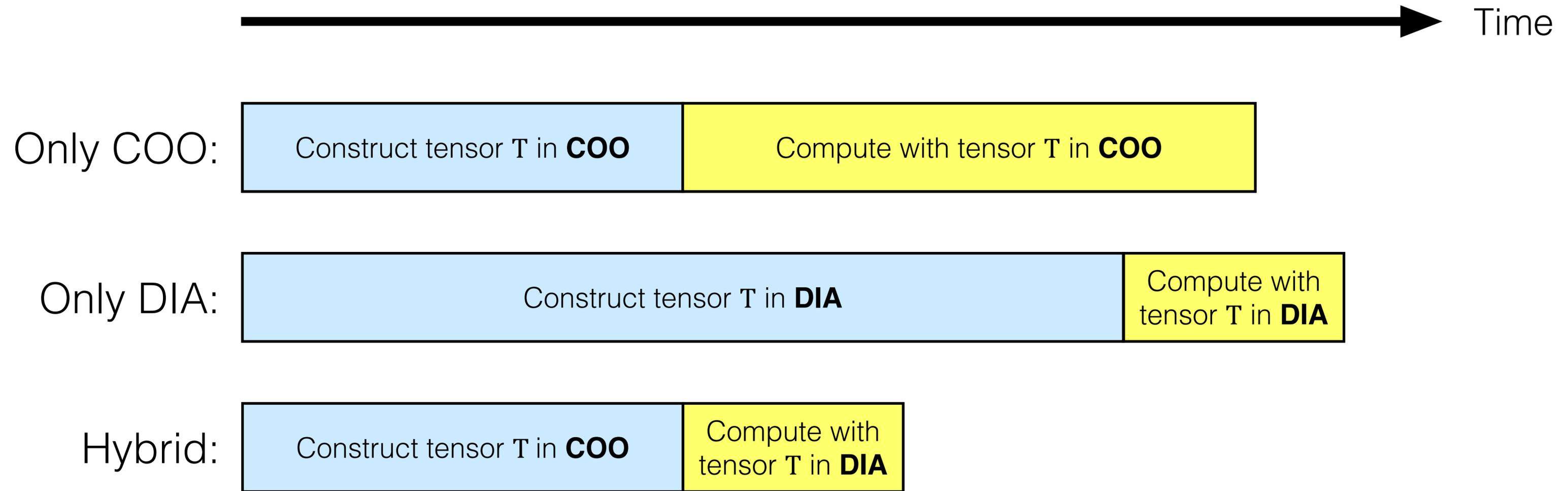
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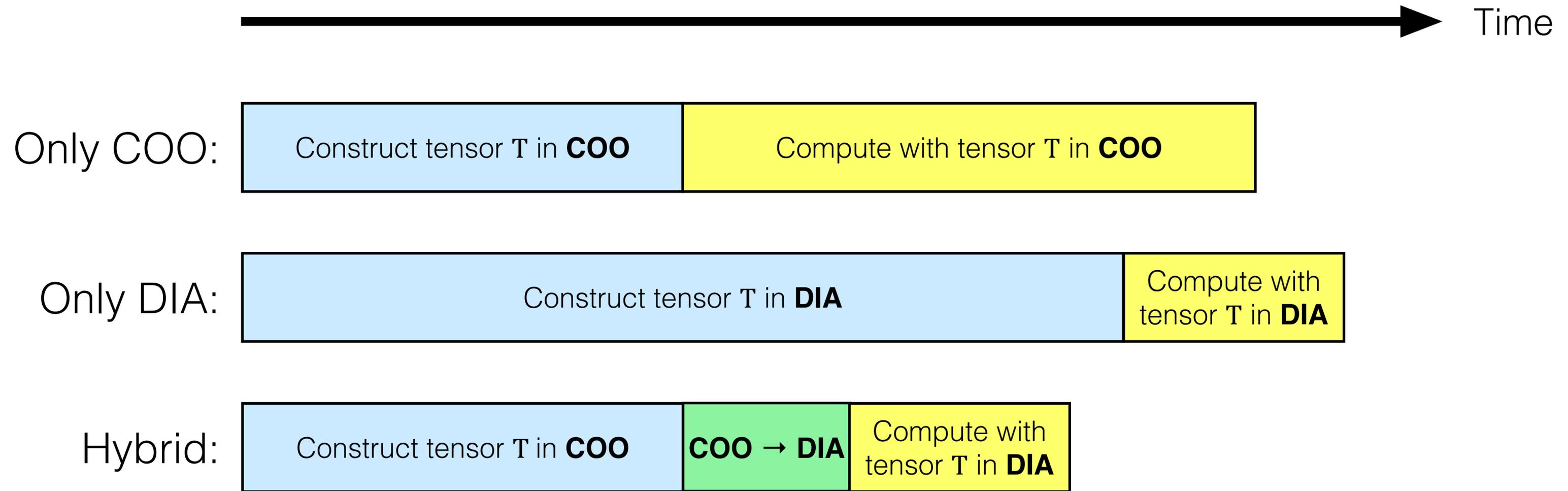
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Applications must work with tensors in different formats for performance



Applications must work with tensors in different formats for performance



Manually implementing support for efficient conversion between all combinations of formats is infeasible

COO

BCSR

ELL

BND

DIA

JAD

SKY

CSR

⋮

COO

BCSR

ELL

BND

DIA

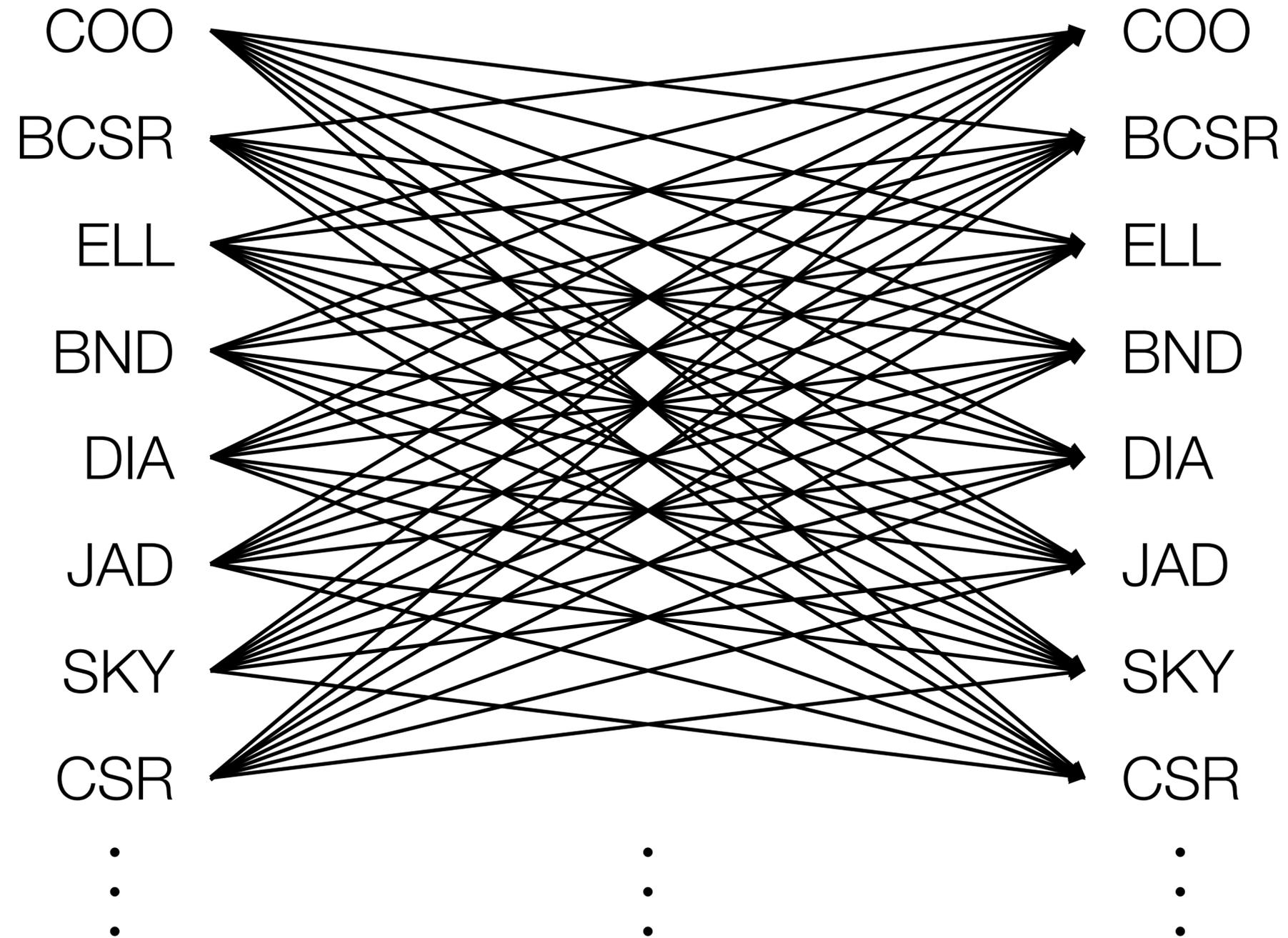
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Manually implementing support for efficient conversion between all combinations of formats is infeasible

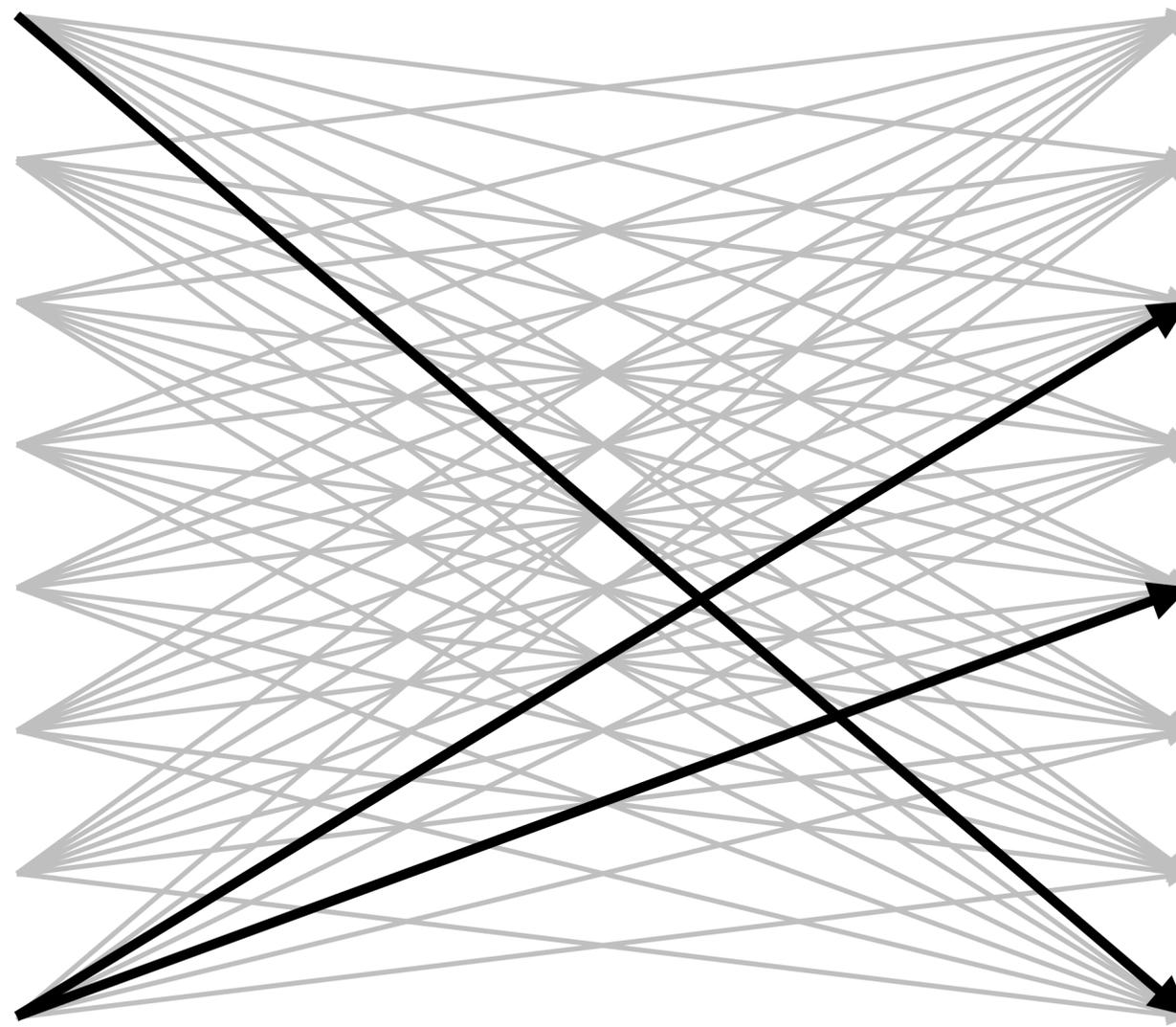
```

int K = 0;
for (int i = 0; i < N; i++) {
    int ncols = A_pos[i+1] - A_pos[i];
    K = max(K, ncols);
}
int* B_crd = new int[K * N]();
double* B_vals = new double[K * N]();
for (int i = 0; i < N; i++) {
    int count = 0;
    for (int pA2 = A_pos[i];
         pA2 < A_pos[i+1]; pA2++) {
        int j = A_crd[pA2];
        int k = count++;
        int pB2 = k * N + i;
        B_crd[pB2] = j;
        B_vals[pB2] = A_vals[pA2];
    }
}

int count[N] = {0};
for (int pA1 = A_pos[0];
     pA1 < A_pos[1]; pA1++) {
    int i = A1_crd[pA1];
    count[i]++;
}
int* B_pos = new int[N + 1];
B_pos[0] = 0;
for (int i = 0; i < N; i++) {
    B_pos[i + 1] = B_pos[i] + count[i];
}
int* B_crd = new int[pos[N]];
double* B_vals = new double[pos[N]];
for (int pA1 = A_pos[0];
     pA1 < A_pos[1]; pA1++) {
    int i = A1_crd[pA1];
    int j = A2_crd[pA1];
    int pB2 = pos[i]++;
    B_crd[pB2] = j;
    B_vals[pB2] = A_vals[pA2];
}
for (int i = 0; i < N; i++) {
    B_pos[N - i] = B_pos[N - i - 1];
}
B_pos[0] = 0;

```

COO
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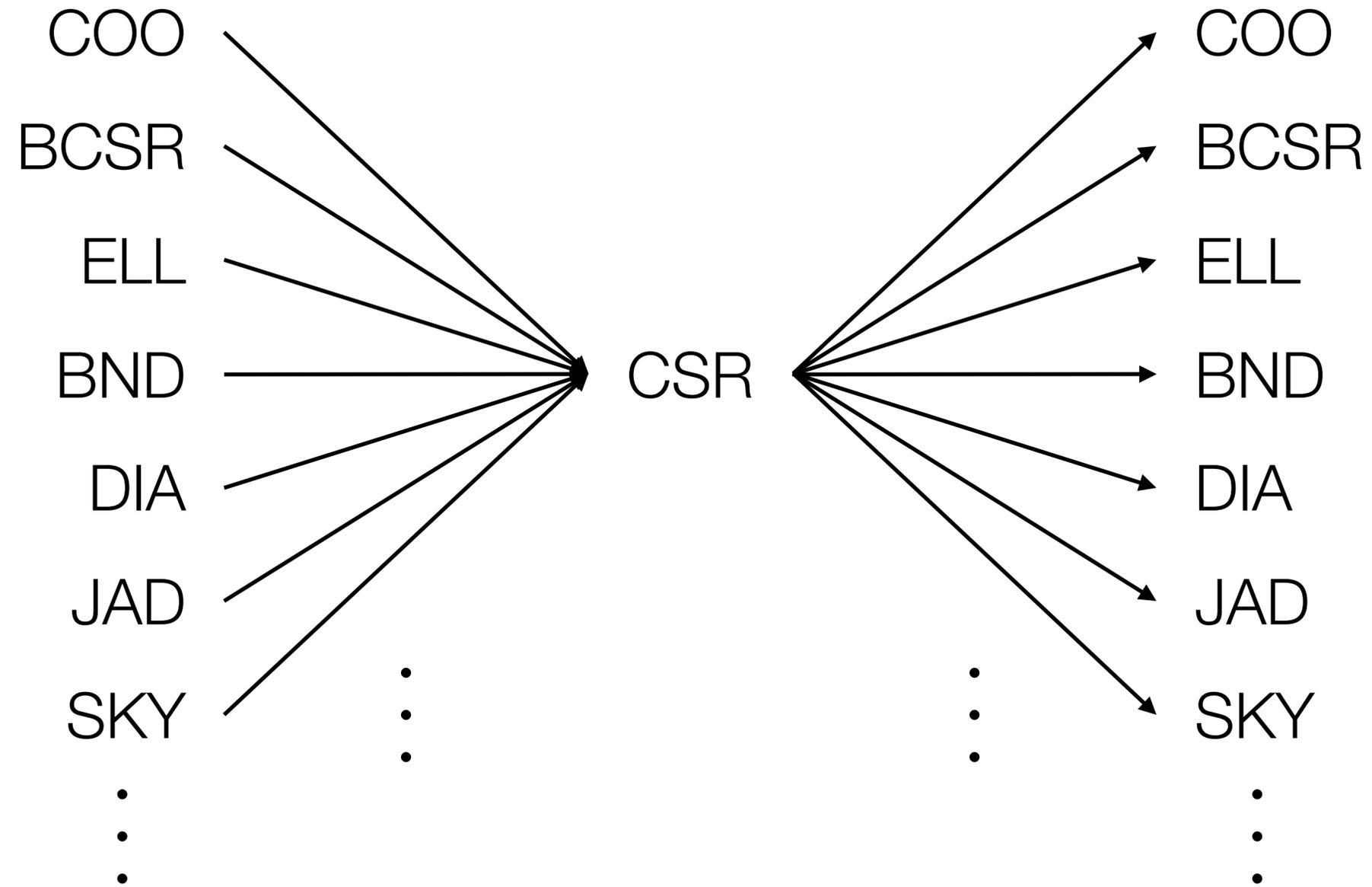
```

bool nz[2 * N - 1] = {0};
for (int i = 0; i < N; i++) {
    for (int pA2 = A_pos[i];
         pA2 < A_pos[i+1]; pA2++) {
        int j = A_crd[pA2];
        int k = j - i;
        nz[k + N - 1] = true;
    }
}
int* B_perm = new int[2 * N - 1];
int K = 0;
for (int i = -N + 1; i < N; i++) {
    if (nz[i + N - 1])
        B_perm[K++] = i;
}
double* B_vals = new double[K * N]();
int* B_rperm = new int[2 * N - 1];
for (int i = 0; i < K; i++) {
    B_rperm[B_perm[i] + N - 1] = i;
}
for (int i = 0; i < N; i++) {
    for (int pA2 = A_pos[i];
         pA2 < A_pos[i+1]; pA2++) {
        int j = A_crd[pA2];
        int k = j - i;
        int pB1 = B_rperm[k + N - 1];
        int pB2 = pB1 * N + i;
        B_vals[pB2] = A_vals[pA2];
    }
}

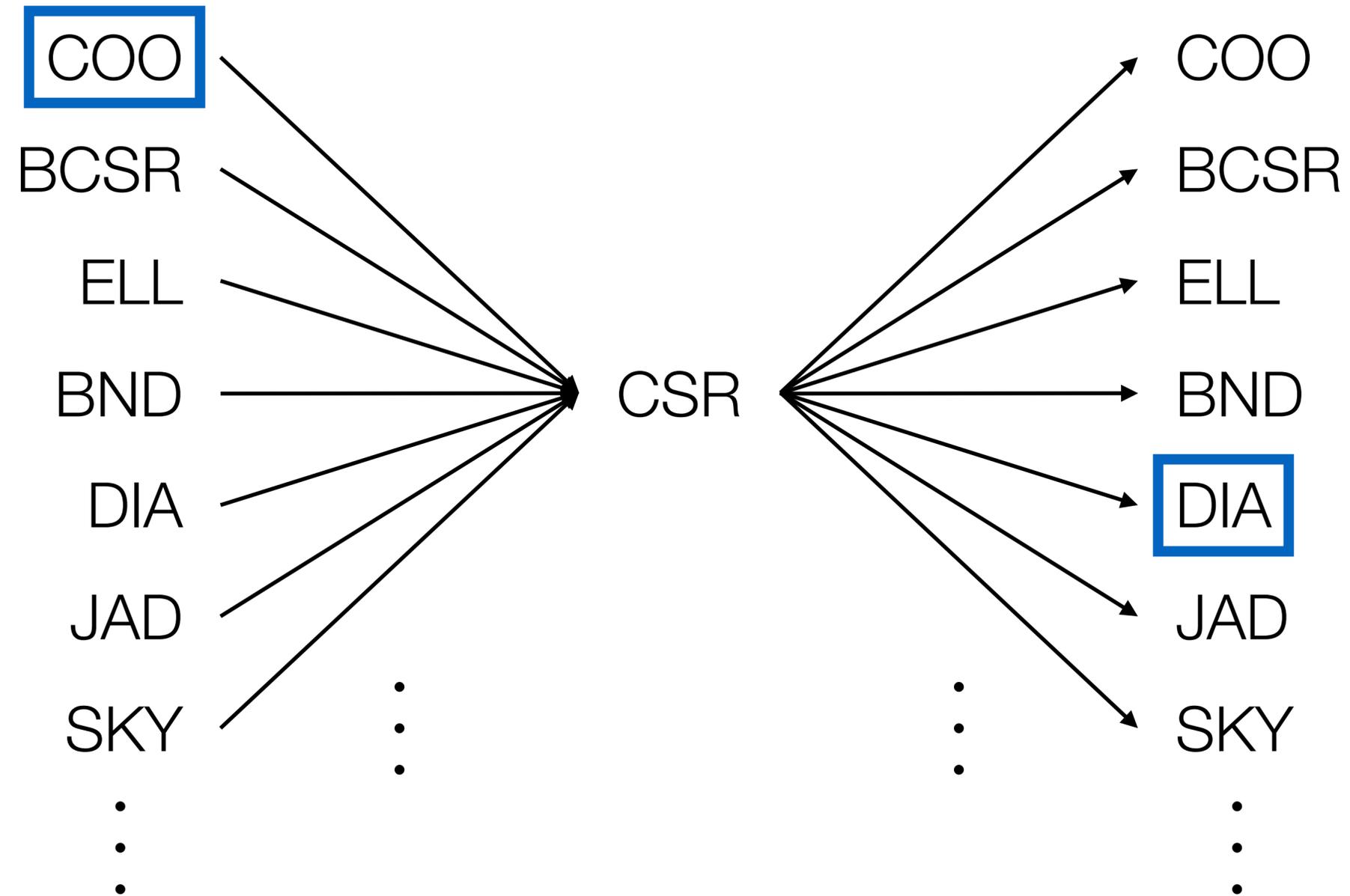
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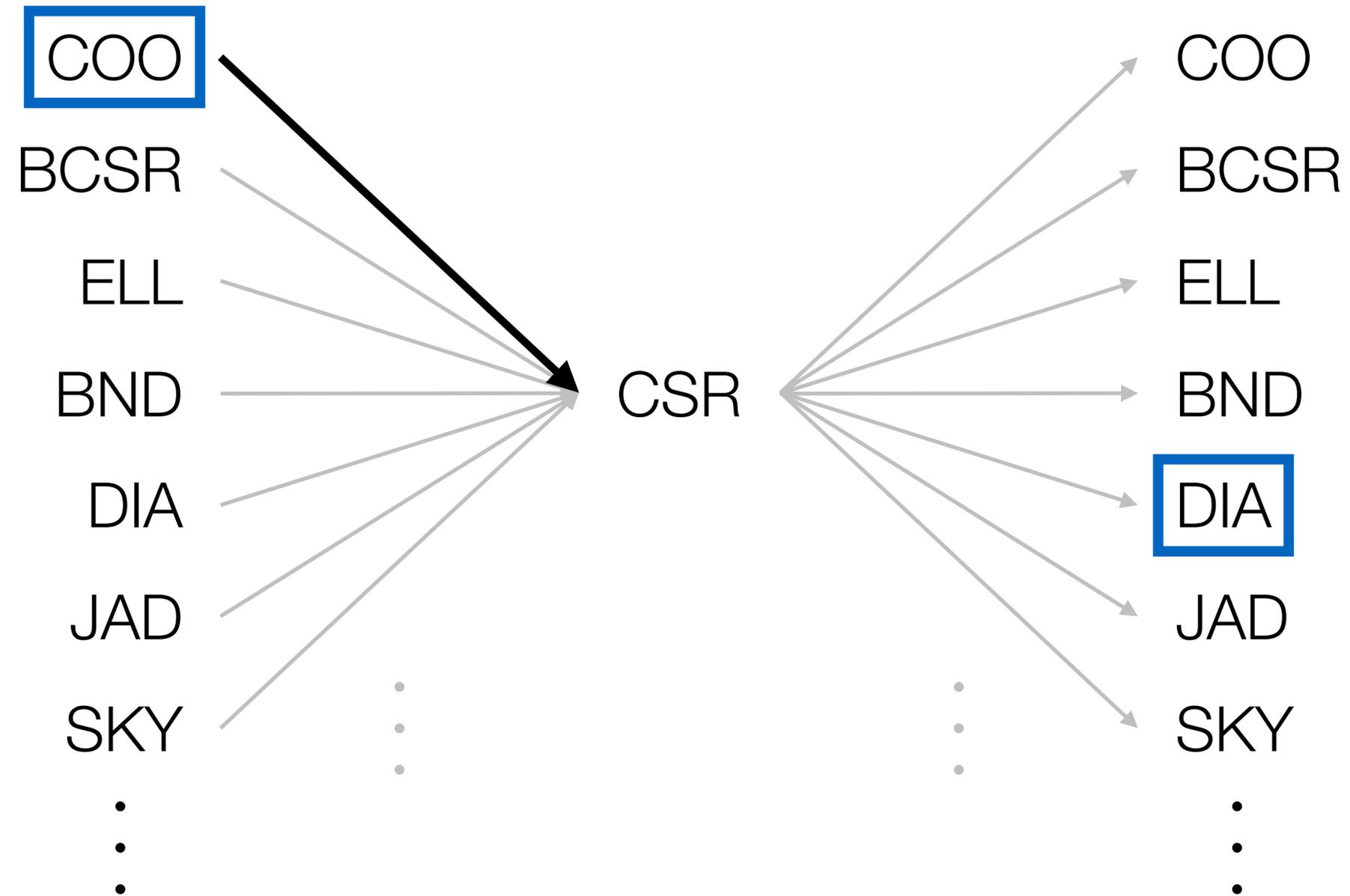
Hand-optimized libraries limit support for efficient conversion to few combinations of formats



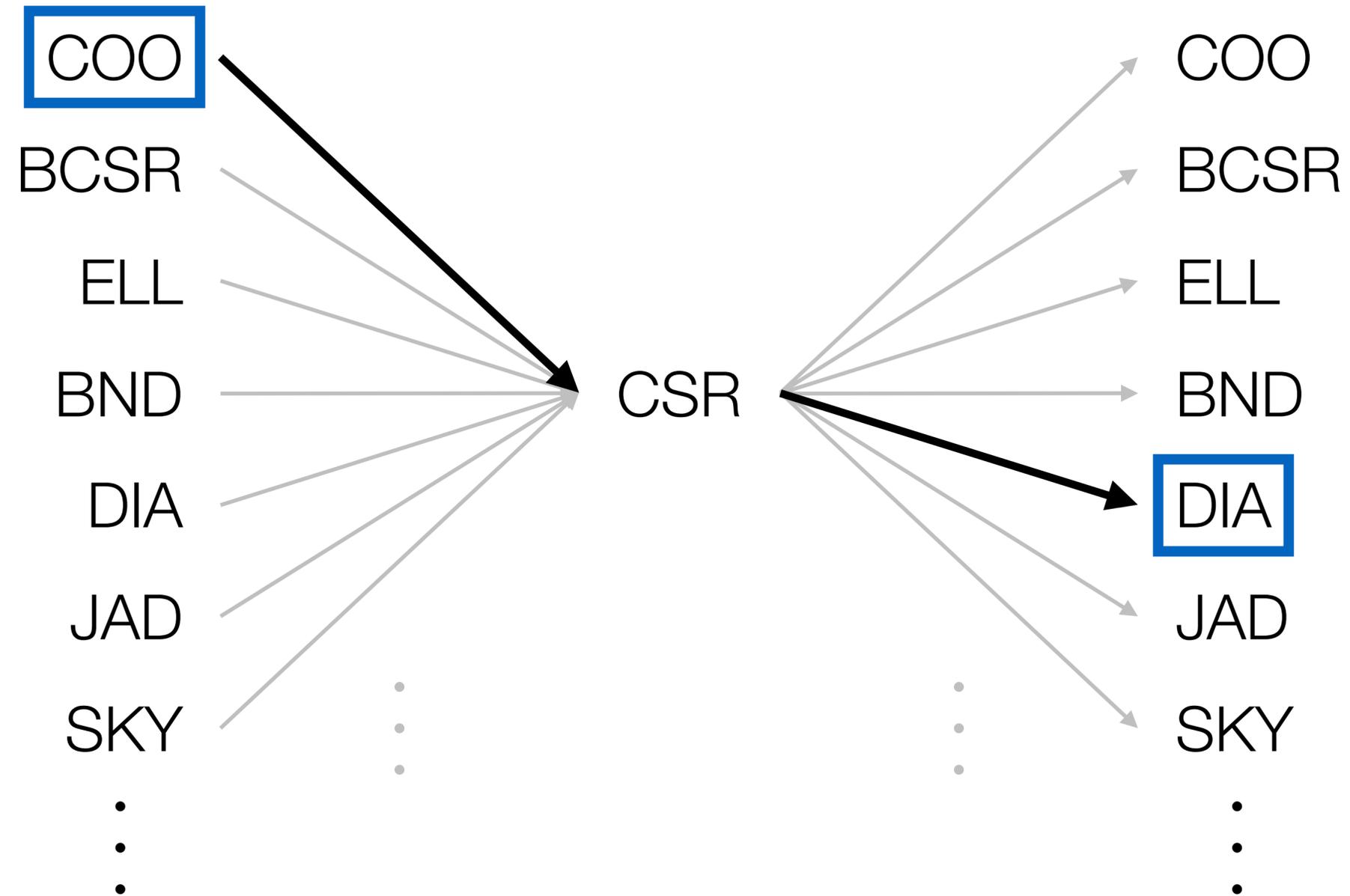
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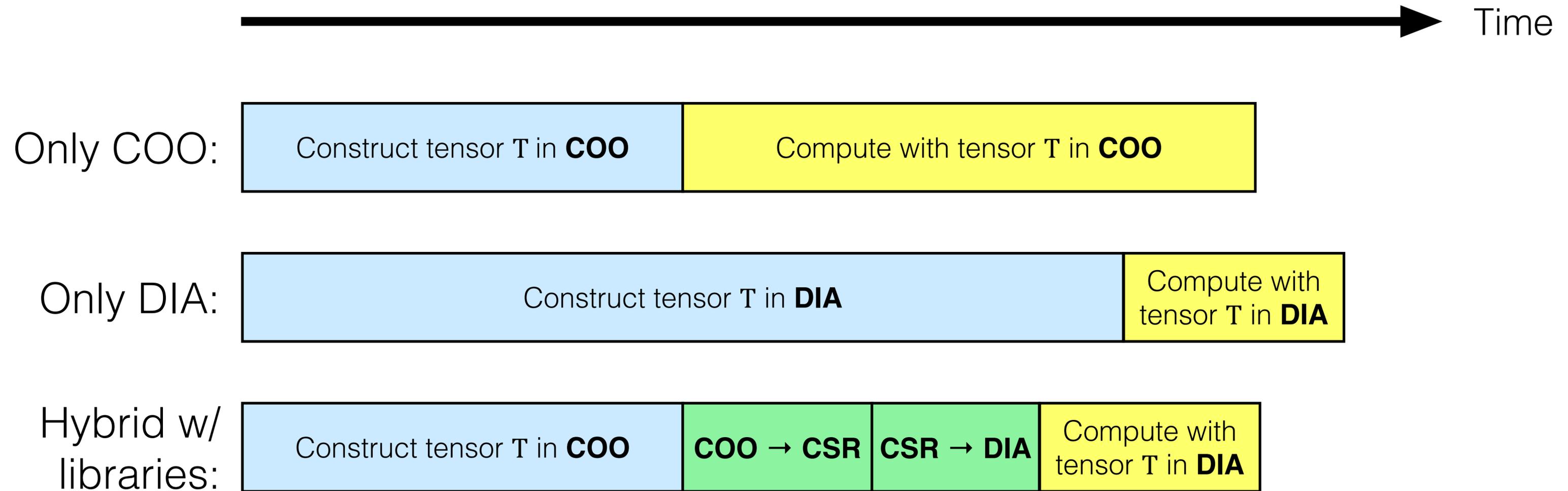
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Hand-optimized libraries limit support for efficient conversion to few combinations of formats



Inefficient conversion eliminates benefit of using different formats

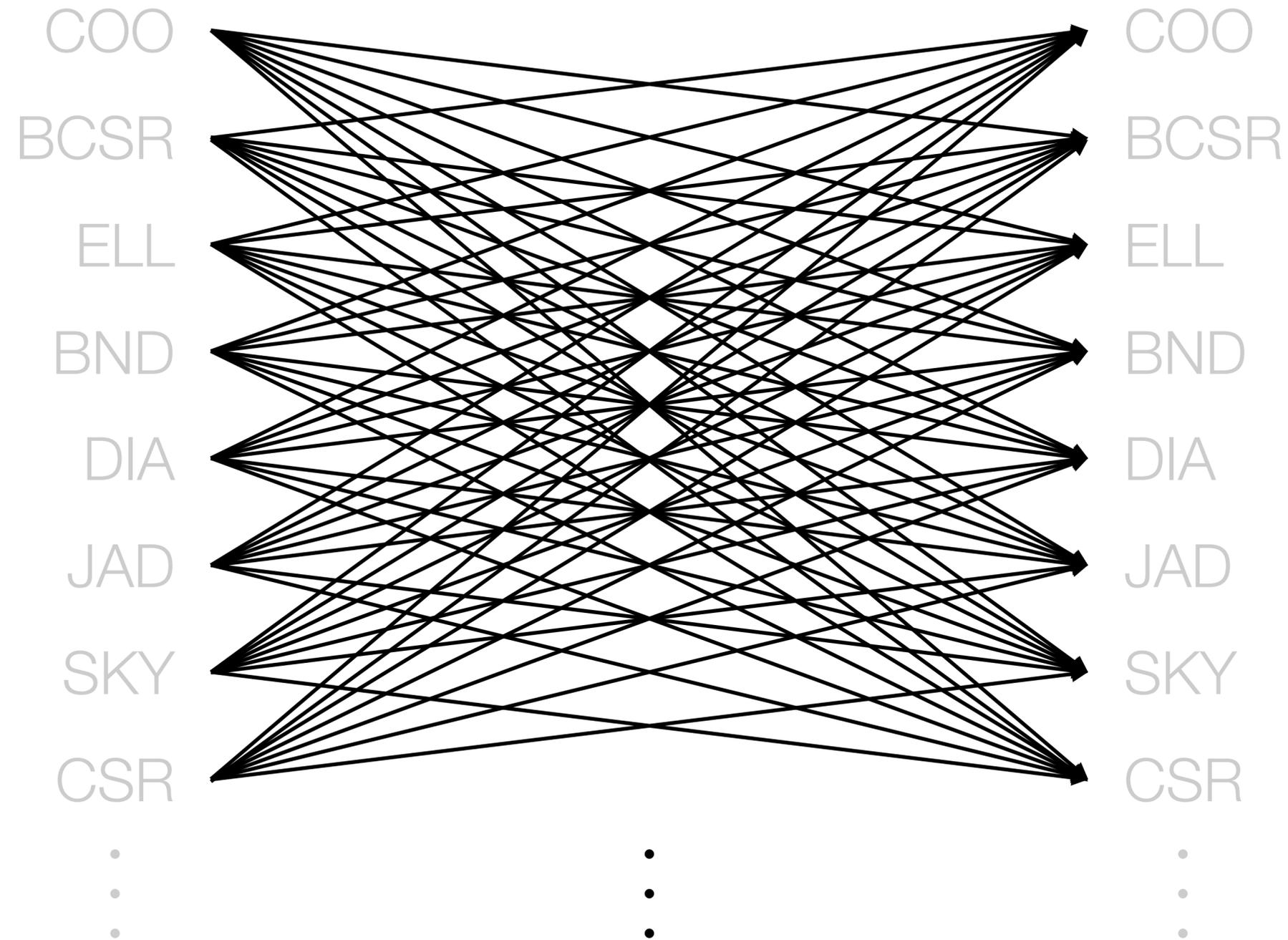


Automatic Generation of Efficient Sparse Tensor Format Conversion Routines

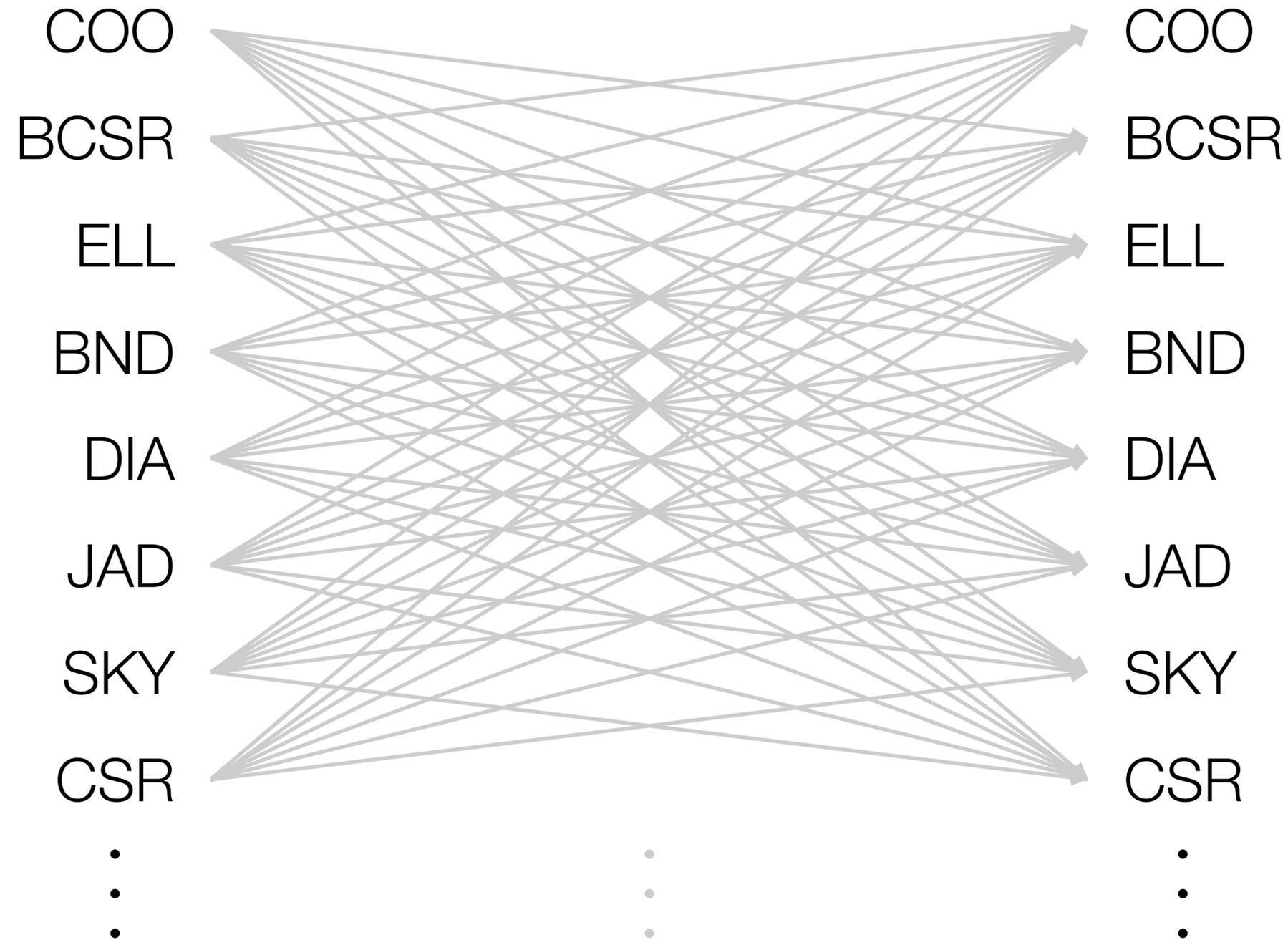
Stephen Chou, Fredrik Kjolstad, and Saman Amarasinghe



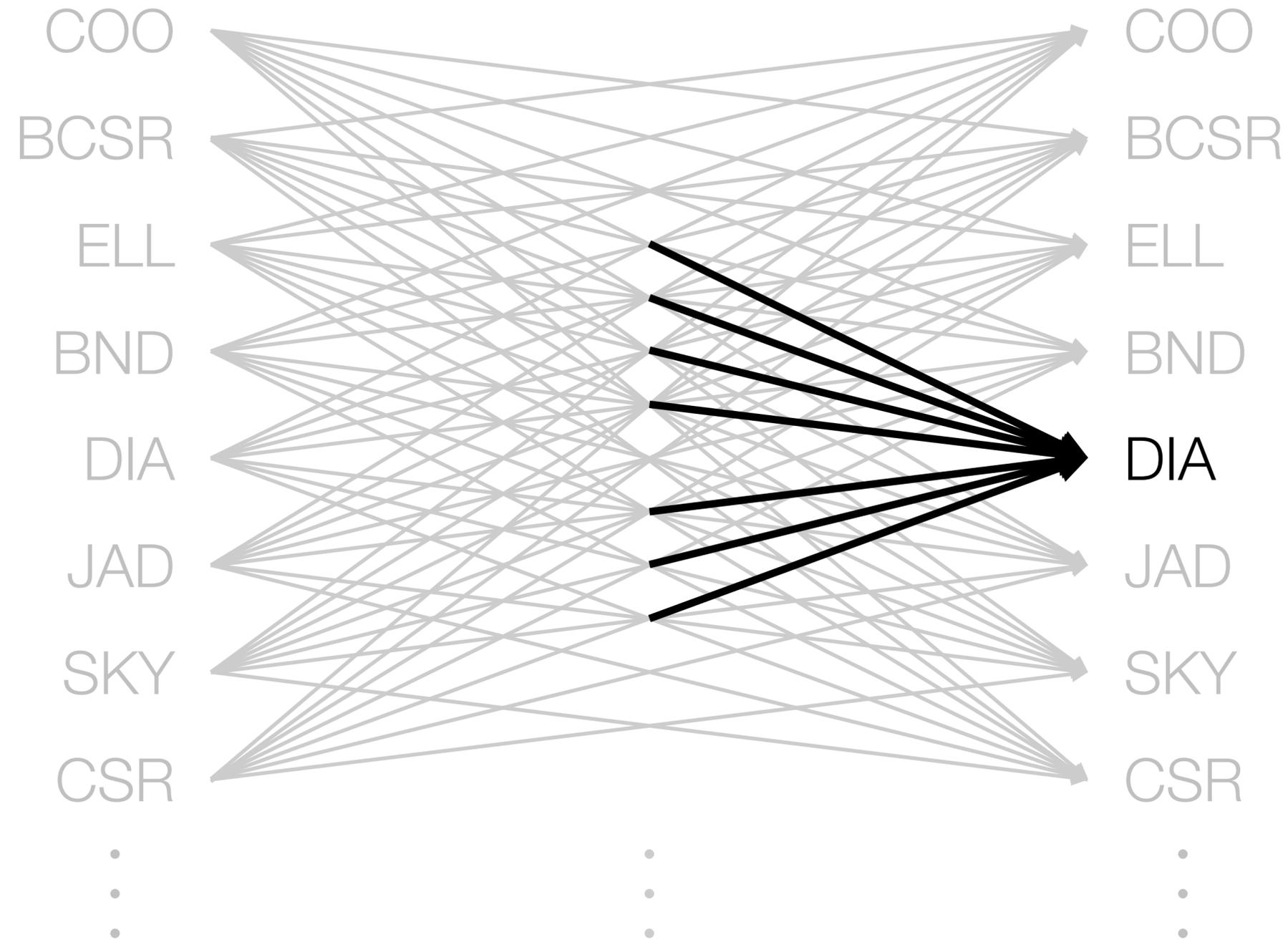
A compiler can generate efficient conversion routines from standalone specifications for each tensor format



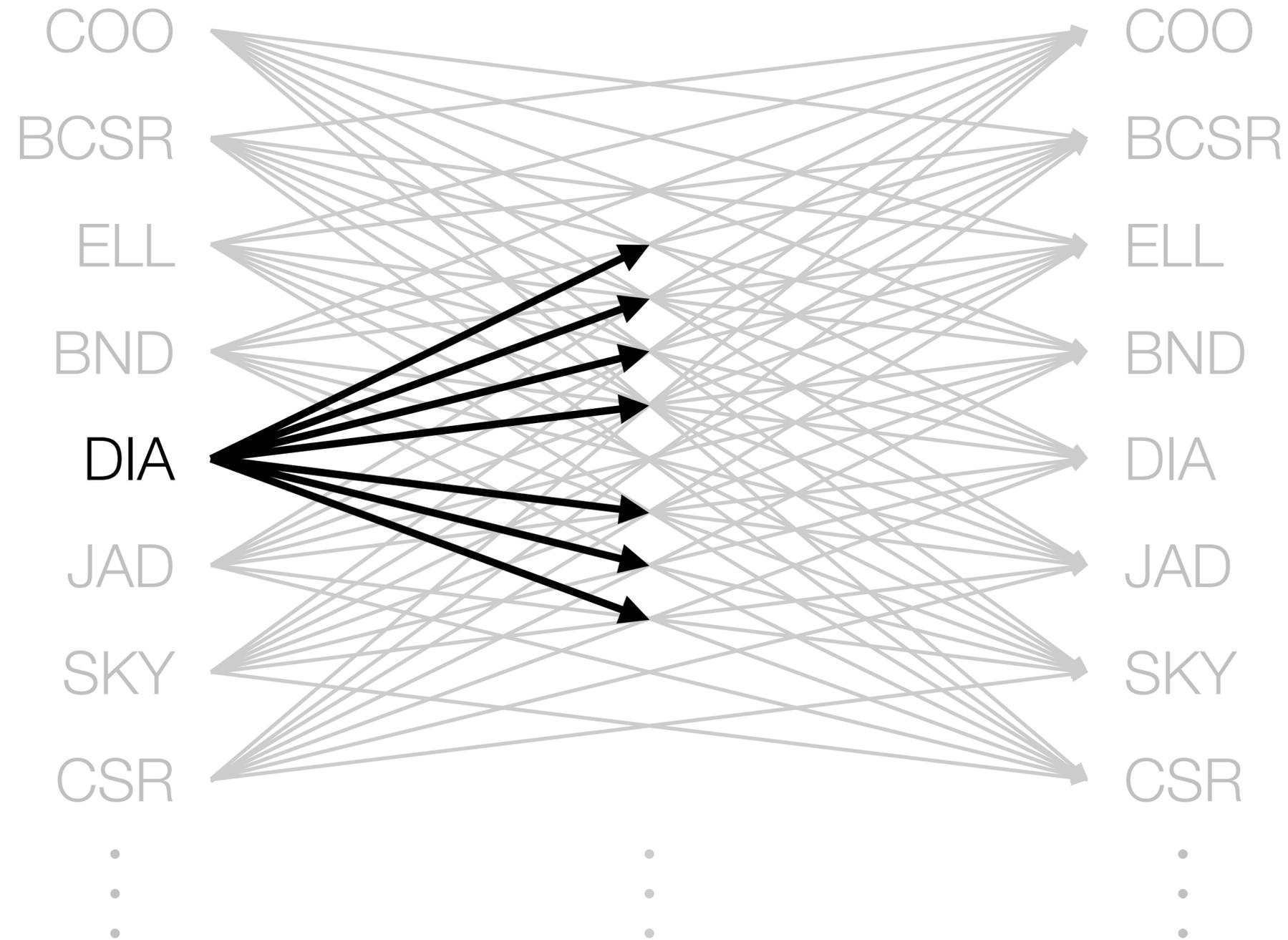
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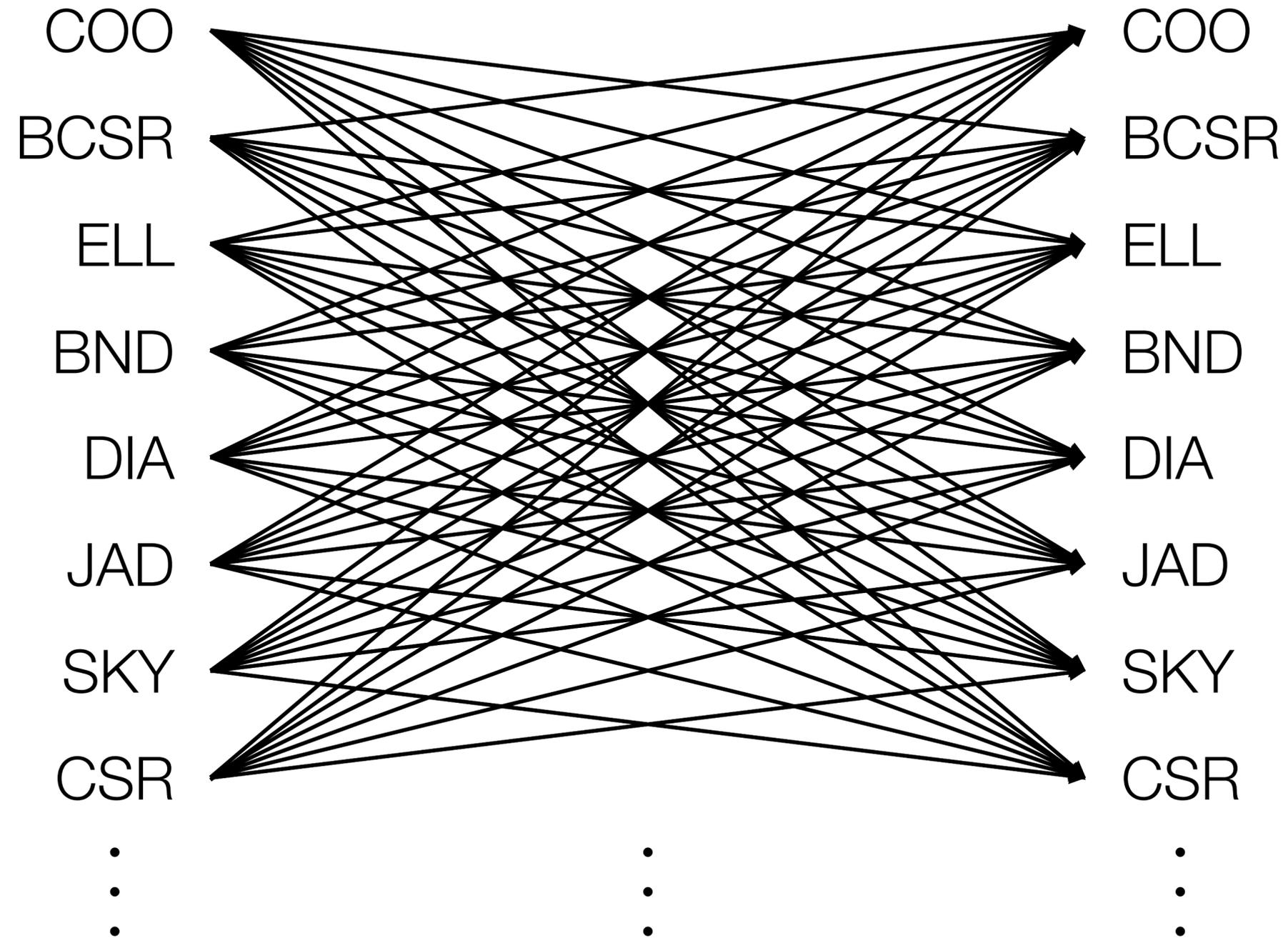
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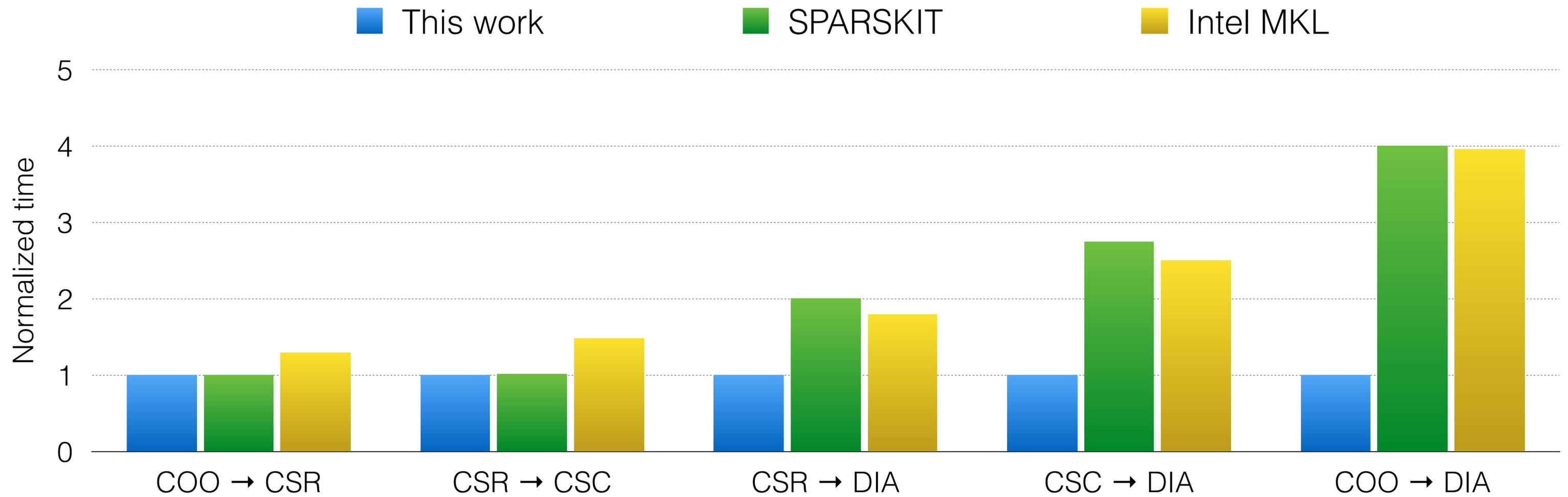
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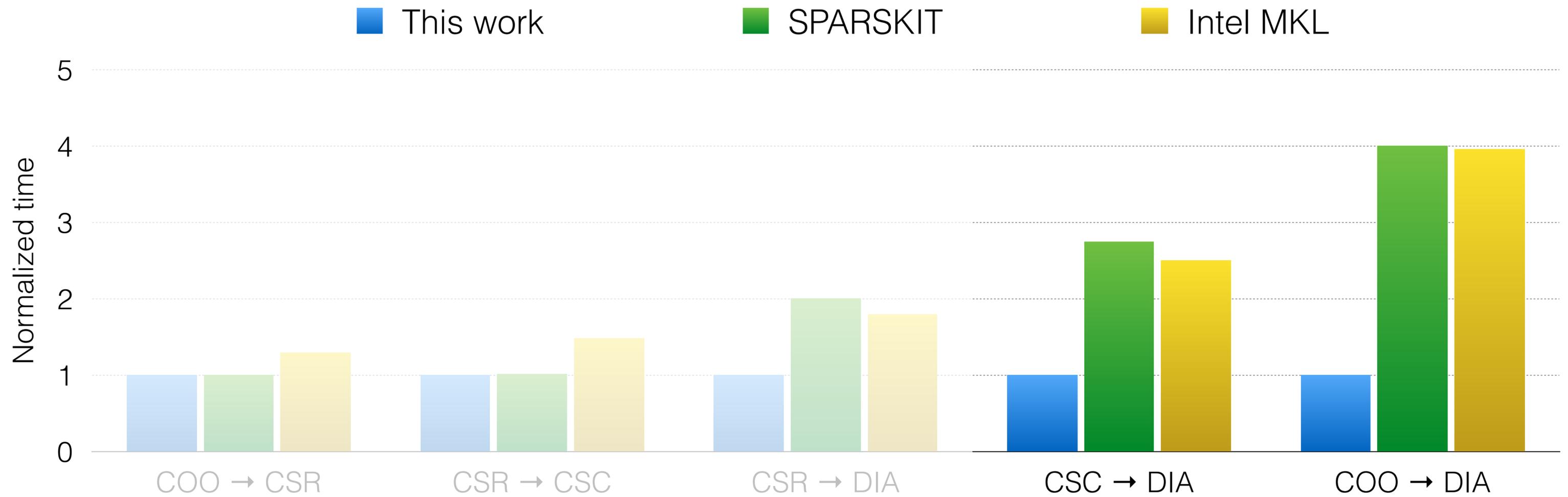
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Our technique generates efficient code



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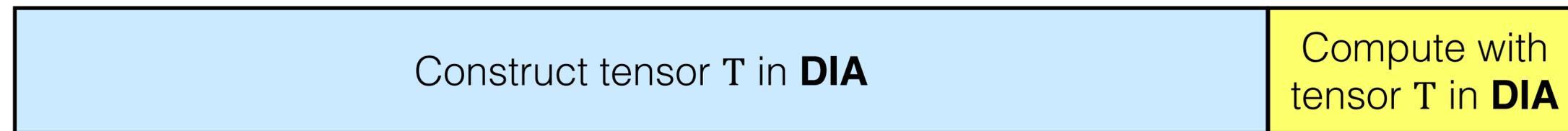
Being able to generate efficient conversion routines lets users exploit different formats for performance



Only COO:



Only DIA:



Hybrid w/
libraries:



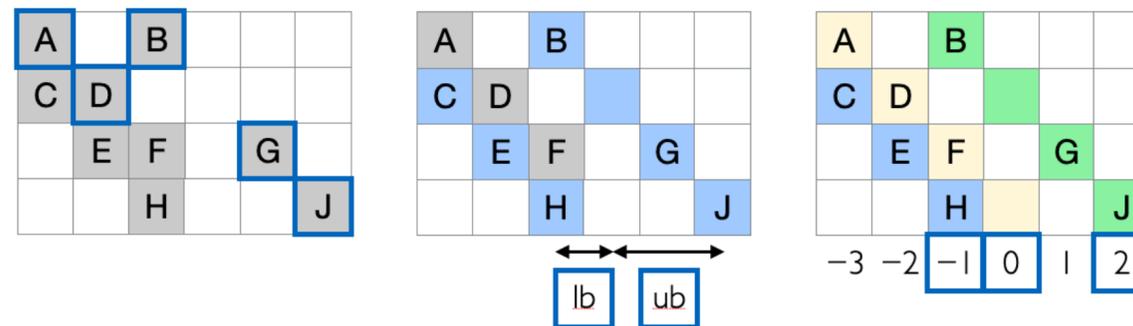
**Hybrid w/
our approach:**



Coordinate Remappings

j-i	-1	-1	-1	0	0	0	2	2	2
i	1	2	3	0	1	2	0	2	3
j	0	1	2	0	1	2	2	4	5
	C	E	H	A	D	F	B	G	J

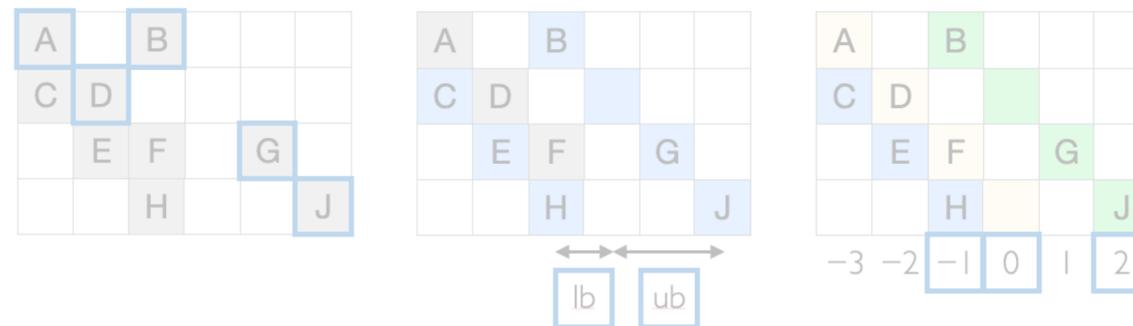
Attribute Queries



Coordinate Remappings

j-i	-1	-1	-1	0	0	0	2	2	2
i	1	2	3	0	1	2	0	2	3
j	0	1	2	0	1	2	2	4	5
	C	E	H	A	D	F	B	G	J

Attribute Queries



Different tensor formats arrange nonzeros in memory in different ways

A		B			
C	D				
	E	F		G	
		H			J

Different tensor formats arrange nonzeros in memory in different ways

pos

0	2	4	7	9
---	---	---	---	---

crd

0	2	1	2	1	2	4	2	5
---	---	---	---	---	---	---	---	---

vals

A	B	C	D	E	F	G	H	J
---	---	---	---	---	---	---	---	---

CSR

A		B			
C	D				
	E	F		G	
		H			J

Different tensor formats arrange nonzeros in memory in different ways

pos

0	2	4	7	9
---	---	---	---	---

crd

0	2	1	2	1	2	4	2	5
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vals

A	B	C	D	E	F	G	H	J
---	---	---	---	---	---	---	---	---

CSR

K

3

N

4

perm

-1	0	2
----	---	---

M

6

vals

	C	E	H	A	D	F		B		G	J
--	---	---	---	---	---	---	--	---	--	---	---

DIA

A		B			
C	D				
	E	F		G	
		H			J

Different tensor formats arrange nonzeros in memory in different ways

pos

0	2	4	7	9
---	---	---	---	---

 crd

0	2	1	2	1	2	4	2	5
---	---	---	---	---	---	---	---	---

 vals

A	B	C	D	E	F	G	H	J
---	---	---	---	---	---	---	---	---

K

3

 N

4

 perm

-1	0	2
----	---	---

 M

6

 vals

	C	E	H	A	D	F		B		G	J
--	---	---	---	---	---	---	--	---	--	---	---

CSR

DIA

A		B			
C	D				
	E	F		G	
		H			J

pos

0	1	3
---	---	---

 BI

2

 crd

0	0	1
---	---	---

 BJ

3

 vals

A		B	C	D			E	F		H		G			J
---	--	---	---	---	--	--	---	---	--	---	--	---	--	--	---

BCSR

Coordinate remapping captures how nonzeros are arranged in memory

	$j = 0$	1	2	3	4	5
$i = 0$	A		B			
1	C	D				
2		E	F		G	
3			H			J

Coordinate remapping captures how nonzeros are arranged in memory

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

i	0	0	1	1	2	2	2	3	3
j	0	2	0	1	1	2	4	2	5
	A	B	C	D	E	F	G	H	J

Coordinate remapping captures how nonzeros are arranged in memory

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

j-i	0	2	-1	0	-1	0	2	-1	2
i	0	0	1	1	2	2	2	3	3
j	0	2	0	1	1	2	4	2	5
	A	B	C	D	E	F	G	H	J

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1	C	D				
2		E	F		G	
3			H			J

j-i	-1	-1	-1	0	0	0	2	2	2
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i	1	2	3	0	1	2	0	2	3
j	0	1	2	0	1	2	2	4	5
	C	E	H	A	D	F	B	G	J

Coordinate remapping captures how nonzeros are arranged in memory



$$(i, j) \rightarrow (j-i, i, j)$$

Coordinate remapping captures how nonzeros are arranged in memory



$$(i, j) \rightarrow (j-i, i, j)$$

Coordinate remapping captures how nonzeros are arranged in memory



$$(i, j) \rightarrow (j-i, \boxed{i, j})$$

Compiler uses coordinate remapping to generate code to reorder nonzeros

$$(i, j) \rightarrow (j-i, i, j)$$

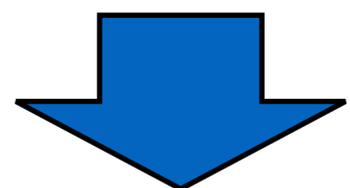
Compiler uses coordinate remapping to generate code to reorder nonzeros

$$(i, j) \rightarrow (j-i, i, j)$$

Identify segment d in `vals`
that corresponds to $j - i$
Identify position p in d
that corresponds to i and j
`vals[p] = B[i,j]`

Compiler uses coordinate remapping to generate code to reorder nonzeros

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J



K 3

N 4

perm -1 0 2

M 6

vals

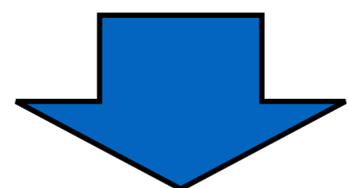
$$(i, j) \rightarrow (j-i, i, j)$$

Identify segment d in vals
that corresponds to $j - i$

Identify position p in d
that corresponds to i and j
vals[p] = B[i, j]

Compiler uses coordinate remapping to generate code to reorder nonzeros

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J



K 3 N 4

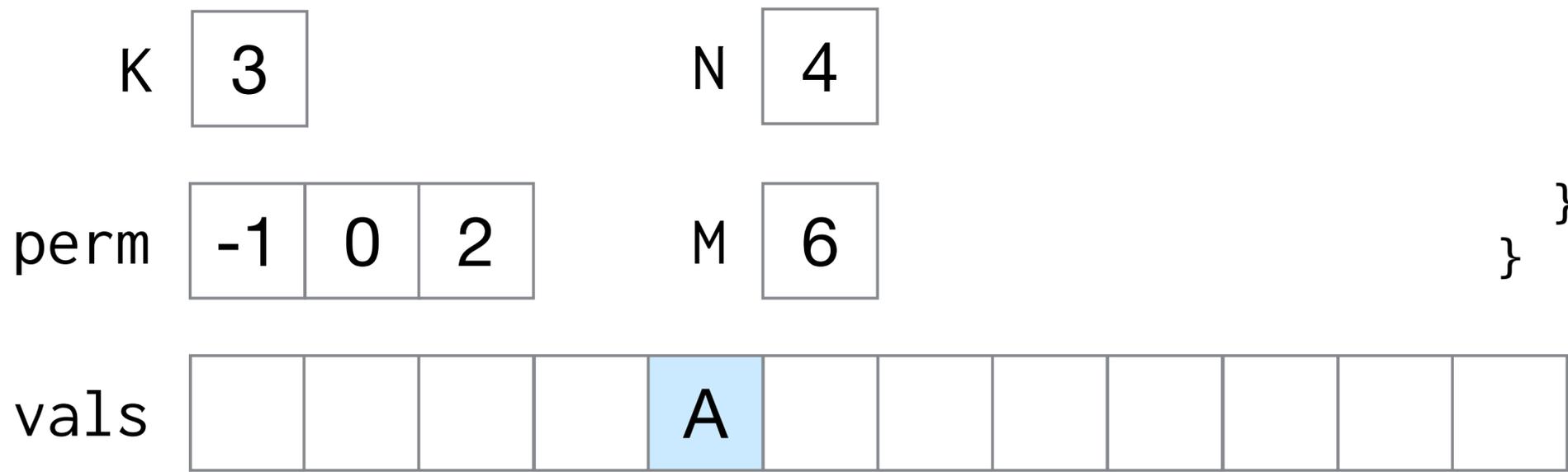
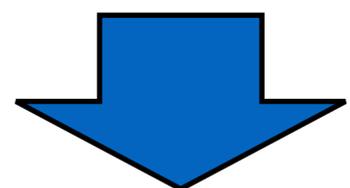
perm -1 0 2 M 6

vals A

$$(i, j) \rightarrow (j-i, i, j)$$

Identify segment d in vals
 that corresponds to $j - i$
 Identify position p in d
 that corresponds to i and j
vals[p] = B[i, j]

Compiler uses coordinate remapping to generate code to reorder nonzeros



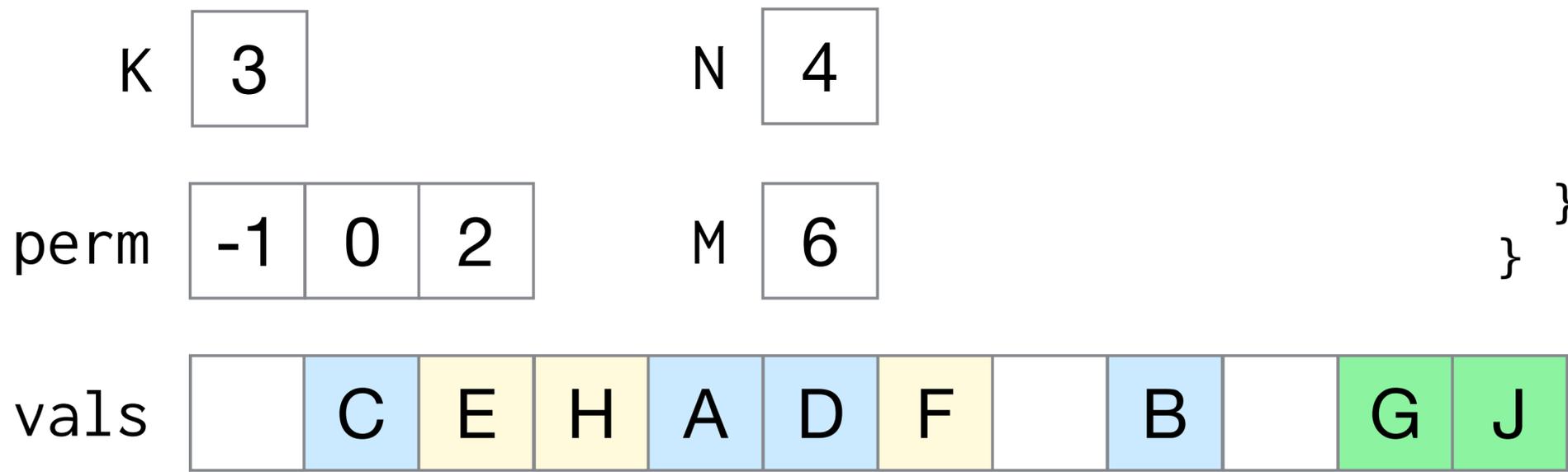
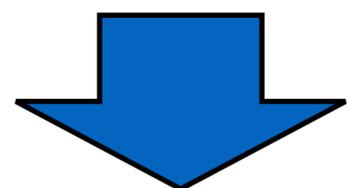
```

for (int bi = 0;
    bi < M / BI; bi++) {
  for (int bj = 0;
      bj < N / BJ; bj++) {
    for (int i = bi * BI;
        i < (bi + 1) * BI; i++) {
      for (int j = bj * BJ;
          j < (bj + 1) * BJ; j++) {
        if (B[i,j] != 0.0) {
          Identify segment d in vals
            that corresponds to j - i
          Identify position p in d
            that corresponds to i and j
          vals[p] = B[i,j]
        }
      }
    }
  }
}

```

Compiler uses coordinate remapping to generate code to reorder nonzeros

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J



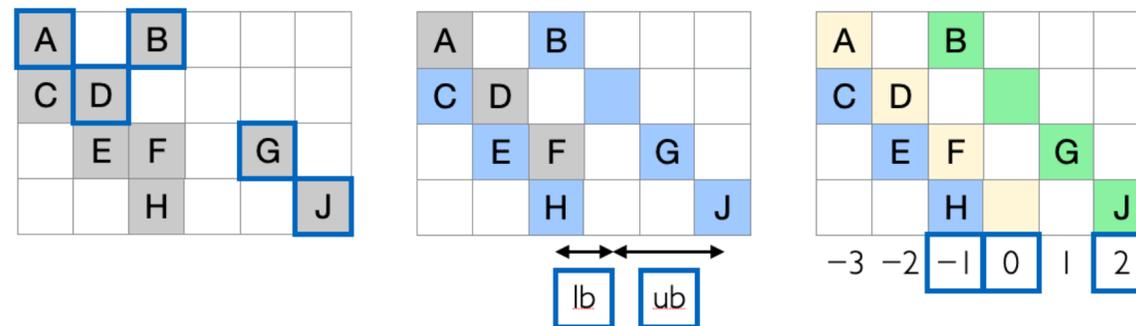
```

for (int bi = 0;
    bi < M / BI; bi++) {
    for (int bj = 0;
        bj < N / BJ; bj++) {
        for (int i = bi * BI;
            i < (bi + 1) * BI; i++) {
            for (int j = bj * BJ;
                j < (bj + 1) * BJ; j++) {
                if (B[i,j] != 0.0) {
                    Identify segment d in vals
                    that corresponds to j - i
                    Identify position p in d
                    that corresponds to i and j
                    vals[p] = B[i,j]
                }
            }
        }
    }
}
    
```

Coordinate Remappings

j-i	-1	-1	-1	0	0	0	2	2	2
i	1	2	3	0	1	2	0	2	3
j	0	1	2	0	1	2	2	4	5
	C	E	H	A	D	F	B	G	J

Attribute Queries



Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

COO

rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

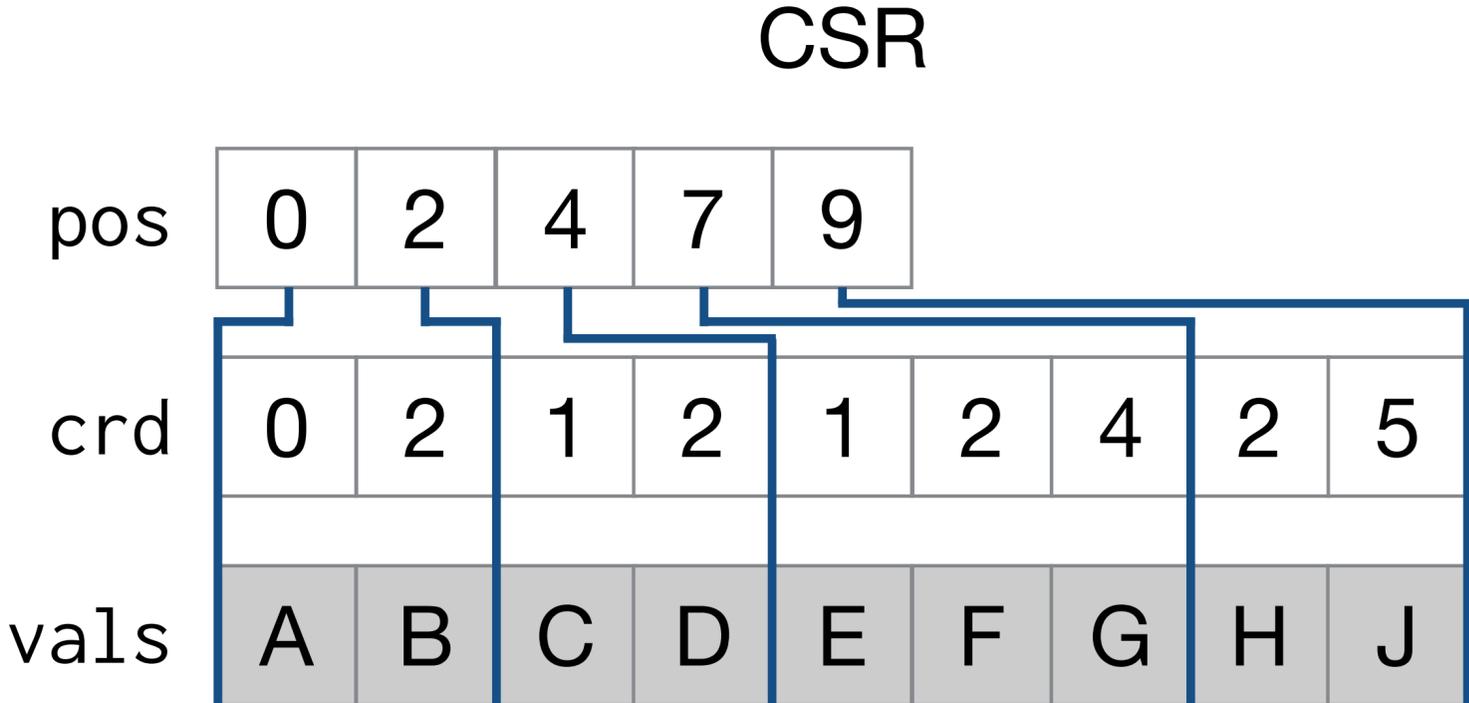
	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

CSR

pos	0	2	4	7	9				
crd	0	2	1	2	1	2	4	2	5
vals	A	B	C	D	E	F	G	H	J

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J



Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

rows

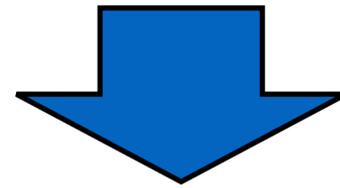
0	1	1	2	0	3	3	2	2
---	---	---	---	---	---	---	---	---

cols

0	0	1	1	2	2	5	2	4
---	---	---	---	---	---	---	---	---

vals

A	C	D	E	B	H	J	F	G
---	---	---	---	---	---	---	---	---



pos

0	0	0	0	0
---	---	---	---	---

crd

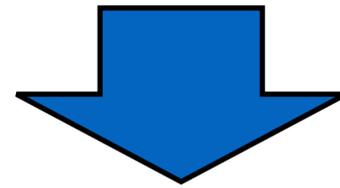
--	--	--	--	--	--	--	--	--

vals

--	--	--	--	--	--	--	--	--

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

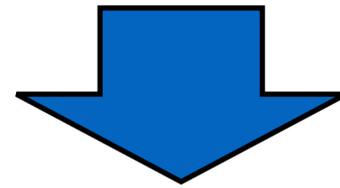
rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G



pos	0	0	0	0	0				
crd	0								
vals	A								

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

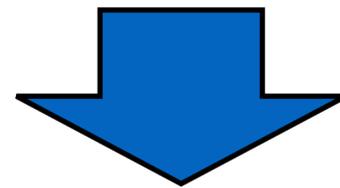
rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G



pos	0	1	1	1	1				
crd	0								
vals	A								

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

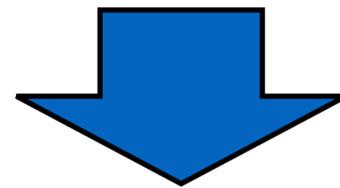
rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G



pos	0	1	3	4	4				
crd	0	0	1	1					
vals	A	C	D	E					

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

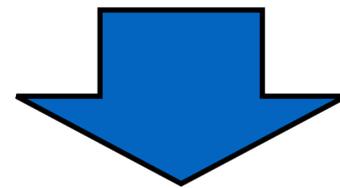
rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G



pos	0	1	3	4	4				
crd	0	0	1	1					
vals	A	C	D	E					

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

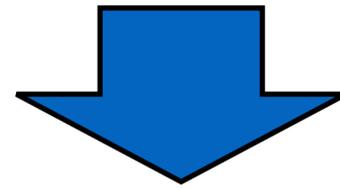
rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G



pos	0	2	4	5	5				
crd	0	2	0	1	1				
vals	A	B	C	D	E				

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G



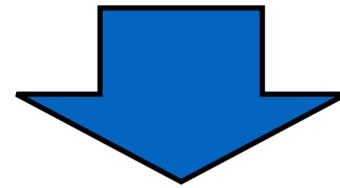
pos	0	2	4	7	9				
crd	0	2	0	1	1	2	4	2	5
vals	A	B	C	D	E	F	G	H	J

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

rows 0 1 1 2 0 3 3 2 2

cols 0 0 1 1 2 2 5 2 4

vals A C D E B H J F G



pos 0

crd

vals

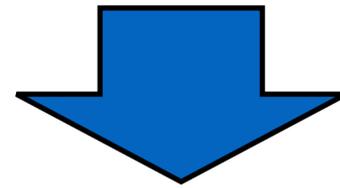
i	nnz
0	2
1	2
2	3
3	2

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

rows 0 1 1 2 0 3 3 2 2

cols 0 0 1 1 2 2 5 2 4

vals A C D E B H J F G



pos 0 2 4 7 9

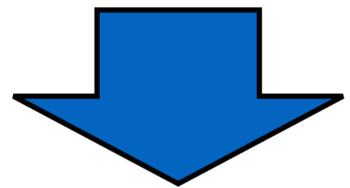
crd

vals

i	nnz
0	2
1	2
2	3
3	2

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G

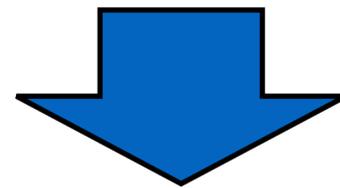


pos	0	2	4	7	9				
crd									
vals									

i	nnz
0	2
1	2
2	3
3	2

Reordering a tensor's nonzeros without explicitly sorting them requires knowing statistics about the tensor

rows	0	1	1	2	0	3	3	2	2
cols	0	0	1	1	2	2	5	2	4
vals	A	C	D	E	B	H	J	F	G



pos	0	2	4	7	9				
crd	0	2	0	1	1	2	4	2	5
vals	A	B	C	D	E	F	G	H	J

i	nnz
0	2
1	2
2	3
3	2

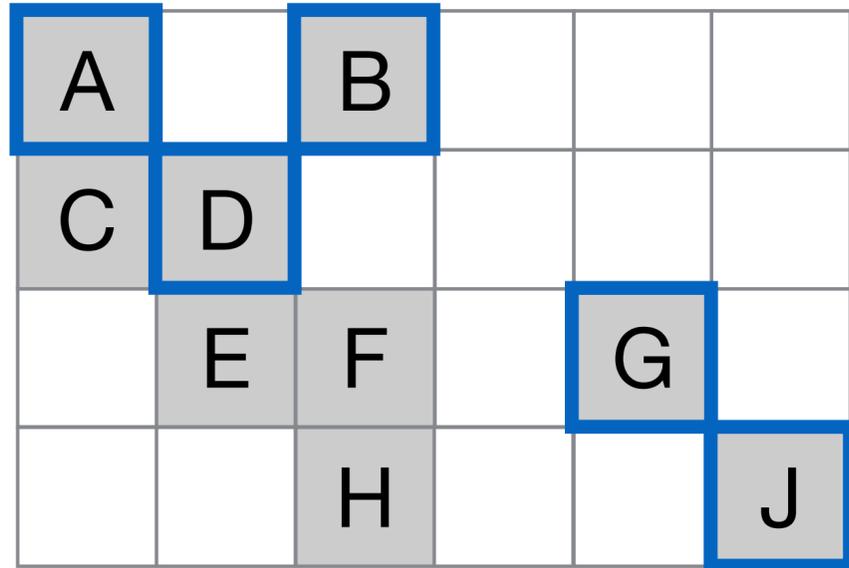
Converting tensors to different formats requires knowing different statistics about the tensors

SKY:

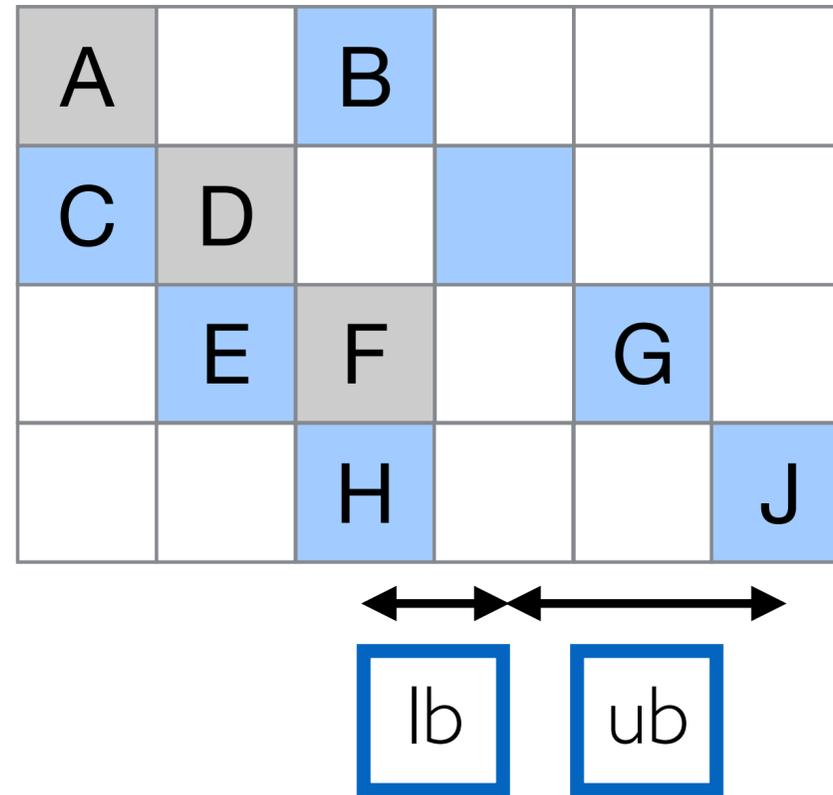
A		B			
C	D				
	E	F		G	
		H			J

Converting tensors to different formats requires knowing different statistics about the tensors

SKY:

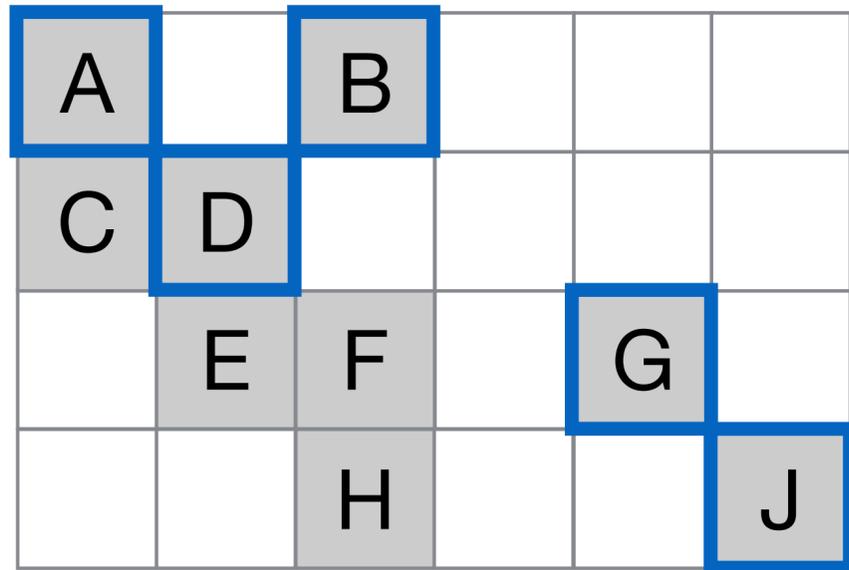


BND:

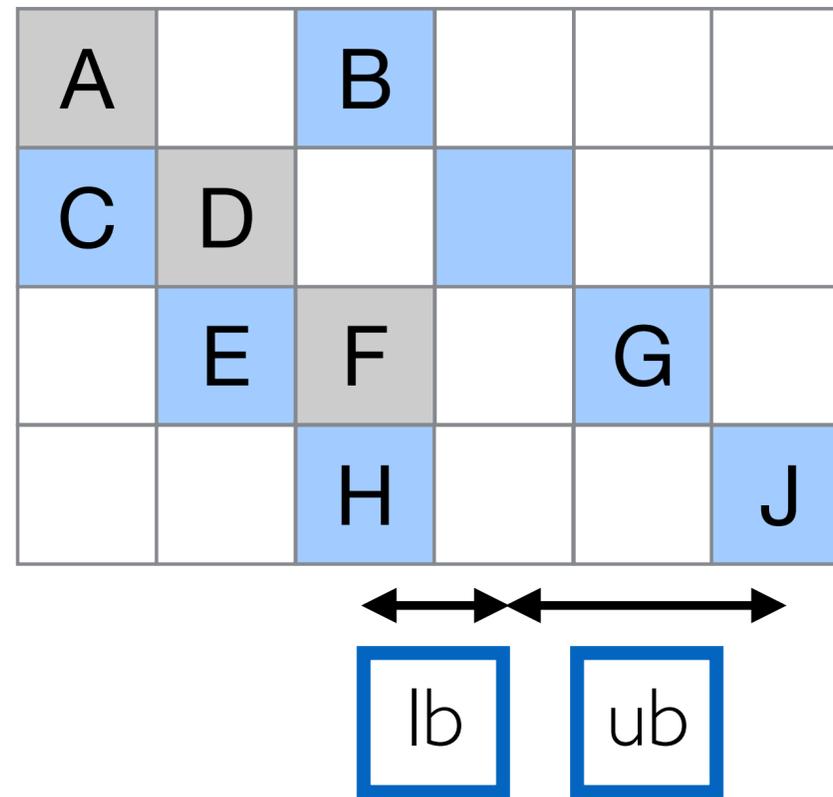


Converting tensors to different formats requires knowing different statistics about the tensors

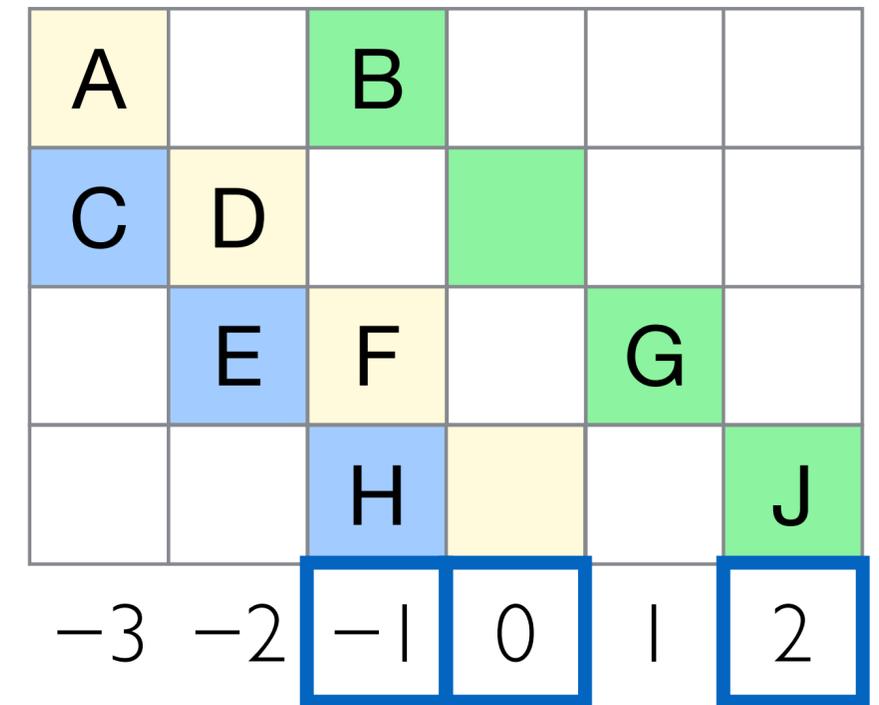
SKY:



BND:



DIA:



Attribute queries express tensor statistics as aggregations over the coordinates of nonzeros

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

```
select [i] -> count(j) as nnz
```

Attribute queries express tensor statistics as aggregations over the coordinates of nonzeros

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

select **[i]** -> count(j) as nnz

Attribute queries express tensor statistics as aggregations over the coordinates of nonzeros

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

select [i] -> **count(j)** as nnz

Attribute queries express tensor statistics as aggregations over the coordinates of nonzeros

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

```
select [i] -> count(j) as nnz
```

i	nnz
0	2
1	2
2	3
3	2

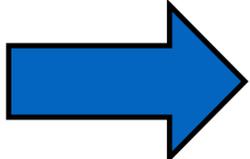
Attribute queries express tensor statistics as aggregations over the coordinates of nonzeros

$j = 0$	1	2	3	4	5
$i = 0$	A		B		
1	C	D			
2		E	F		G
3			H		J

```
select [i] -> count(j) as nnz
```

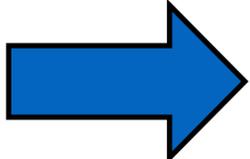
i	nnz
0	2
1	2
2	3
3	2

Compiler generates code to compute attribute queries
by reducing them to sparse tensor computations

`select [i] -> count(j) as Q`  $\forall_i \forall_j Q_i += \text{map}(B_{ij}, 1)$

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

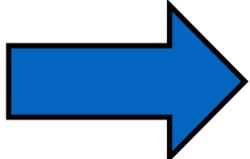
Compiler generates code to compute attribute queries by reducing them to sparse tensor computations

select [i] -> count(j) as Q  $\forall_i \forall_j Q_i += \text{map}(B_{ij}, 1)$

	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

	j = 0	1	2	3	4	5
i = 0	1		1			
1	1	1				
2		1	1		1	
3			1			1

Compiler generates code to compute attribute queries by reducing them to sparse tensor computations

select [i] -> count(j) as Q  $\forall_i \forall_j Q_i += \text{map}(B_{ij}, 1)$

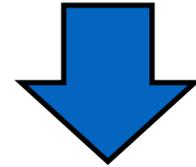
	j = 0	1	2	3	4	5
i = 0	A		B			
1	C	D				
2		E	F		G	
3			H			J

	j = 0	1	2	3	4	5
i = 0	1		1			
1	1	1				
2		1	1		1	
3			1			1

	0	1	2	3
Q	2	2	3	2

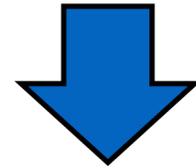
Compiler generates code to compute attribute queries
by reducing them to sparse tensor computations

```
select [i] -> count(j) as Q
```

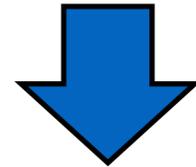

$$\forall_i \forall_j Q_i += \text{map}(B_{ij}, 1)$$

Compiler generates code to compute attribute queries
by reducing them to sparse tensor computations

```
select [i] -> count(j) as Q
```



$$\boxed{\forall_i \forall_j} Q_i += \text{map}(B_{ij}, 1)$$

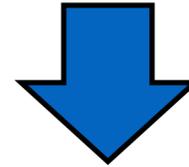


B is CSC

```
for (int j = 0; j < N; j++) {  
  for (int pB = pos[j];  
        pB < pos[j+1]; pB++) {  
    int i = crd[pB2];  
  }  
}
```

Compiler generates code to compute attribute queries
by reducing them to sparse tensor computations

`select [i] -> count(j) as Q`



$$\forall_i \forall_j Q_i += \text{map}(B_{ij}, 1)$$

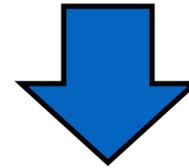


B is CSC

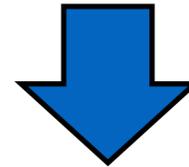
```
for (int j = 0; j < N; j++) {  
  for (int pB = pos[j];  
       pB < pos[j+1]; pB++) {  
    int i = crd[pB2];  
    Q[i] += 1;  
  }  
}
```

Compiler generates code to compute attribute queries by reducing them to sparse tensor computations

select [i] -> count(j) as Q



$$\forall_i \forall_j Q_i += \text{map}(B_{ij}, 1)$$



B is CSC

```
for (int j = 0; j < N; j++) {  
  for (int pB = pos[j];  
       pB < pos[j+1]; pB++) {  
    int i = crd[pB2];  
    Q[i] += 1;  
  }  
}
```

B is COO



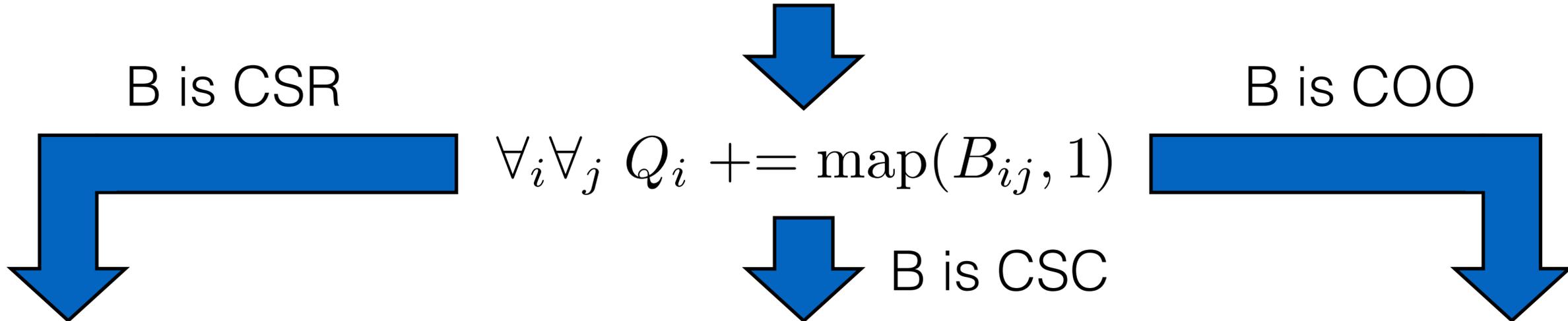
```
for (int pB = 0;  
     pB < NNZ; pB++) {  
  int i = rows[pB];  
  Q[i] += 1;  
}
```

Compiler generates code to compute attribute queries by reducing them to sparse tensor computations

select [i] -> count(j) as Q

B is CSR

B is COO



$B'_i \equiv (\text{pos}[i+1] - \text{pos}[i])$
 $\forall_i Q_i = B'_i$

```

for (int j = 0; j < N; j++) {
  for (int pB = pos[j];
       pB < pos[j+1]; pB++) {
    int i = crd[pB2];
    Q[i] += 1;
  }
}

```

```

for (int pB = 0;
     pB < NNZ; pB++) {
  int i = rows[pB];
  Q[i] += 1;
}

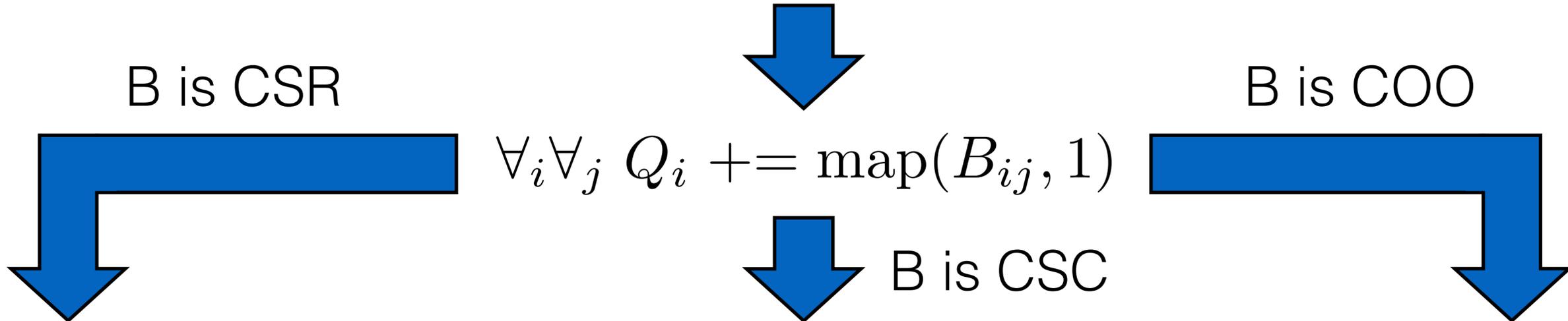
```

Compiler generates code to compute attribute queries by reducing them to sparse tensor computations

select [i] -> count(j) as Q

B is CSR

B is COO



$$\forall_i \forall_j Q_i += \text{map}(B_{ij}, 1)$$

B is CSC

$$B'_i \equiv (\text{pos}[i+1] - \text{pos}[i])$$

$$\forall_i Q_i = B'_i$$

```
for (int j = 0; j < N; j++) {
  for (int pB = pos[j];
       pB < pos[j+1]; pB++) {
    int i = crd[pB2];
    Q[i] += 1;
  }
}
```

```
for (int pB = 0;
     pB < NNZ; pB++) {
  int i = rows[pB];
  Q[i] += 1;
}
```

```
for (int i = 0; i < N; i++) {
  Q[i] = pos[i+1] - pos[i];
}
```

In conclusion...

Efficient sparse tensor conversion routines can be automatically generated from per-format specifications



tensor-compiler.org



This work was supported by:



In conclusion...

Efficient sparse tensor conversion routines can be automatically generated from per-format specifications

Adding support for new sparse tensor formats is straightforward



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Efficient sparse tensor conversion routines can be automatically generated from per-format specifications

Adding support for new sparse tensor formats is straightforward

Our technique makes it simple to fully exploit disparate tensor formats for performance



tensor-compiler.org



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